

Joint Design of GNSS Signal and Message Structure for Galileo 2nd Generation

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- Context: Galileo 2nd Generation (G2G)
- Goal:
 - Improve the acquisition phase
 - Improve the receiver sensitivity
 - Reduce the TTFF*
- Opportunity:
 - Design a new signal to improve the acquisition phase
- Wayforward:
 - Design of a new modulation
 - Design of a new family of PRN* code
 - Co-design of the message structure and the channel coding scheme

PRN* = Pseudo Random Noise

TTFF* = Time To First Fix

- Introduction & background
- Design a new modulation for fast acquisition:
 - BCS
- Design new PRN codes for fast acquisition:
 - Random codes
- Co-design of the message structure and channel coding:
 - Maximum distance separable codes(MDS)
 - Full diversity codes
- Conclusion
- Future Lines

- **Introduction & background**
- Design a new modulation for fast acquisition:
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What is GNSS?

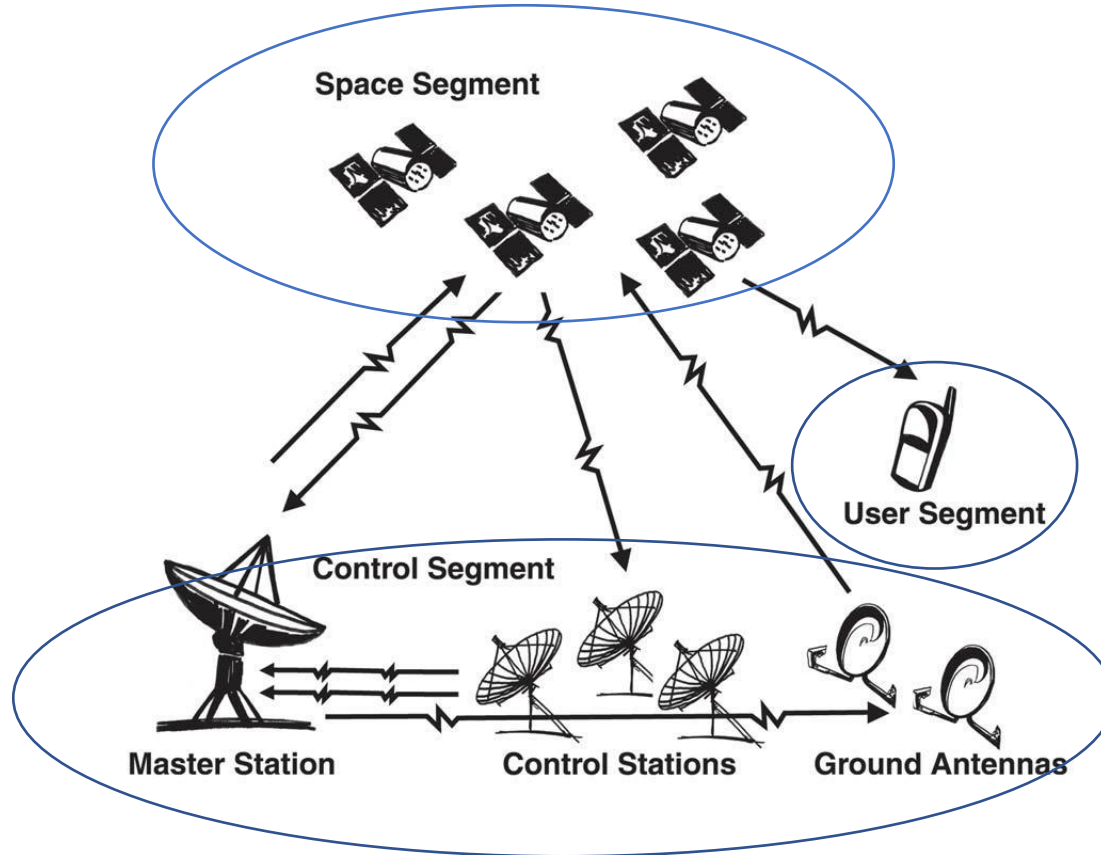
Global Navigation Satellite System



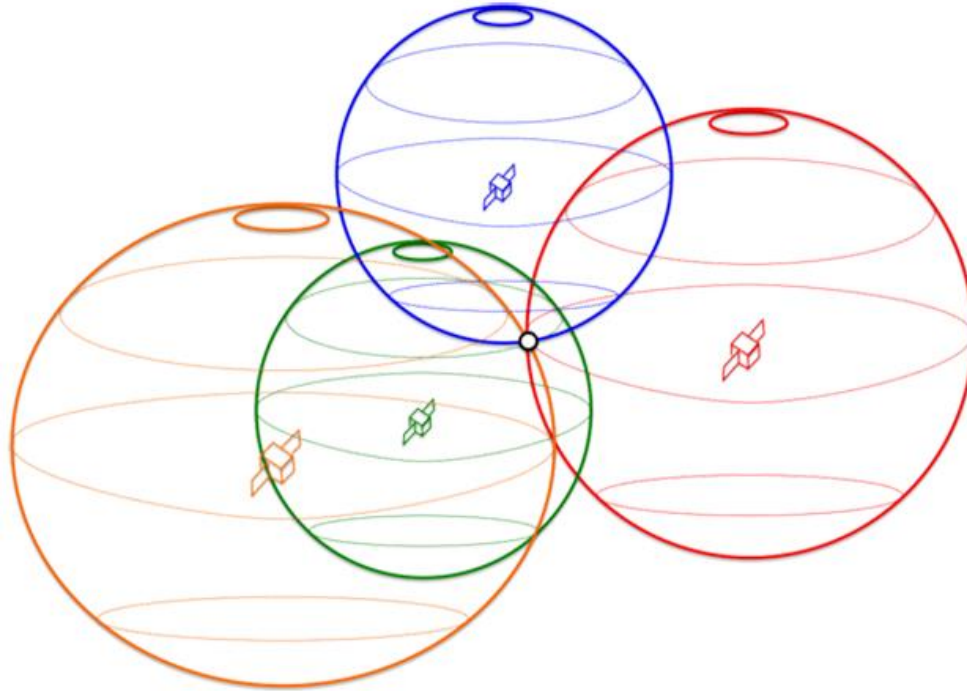
- Position
- Speed
- Time

Global 24/7

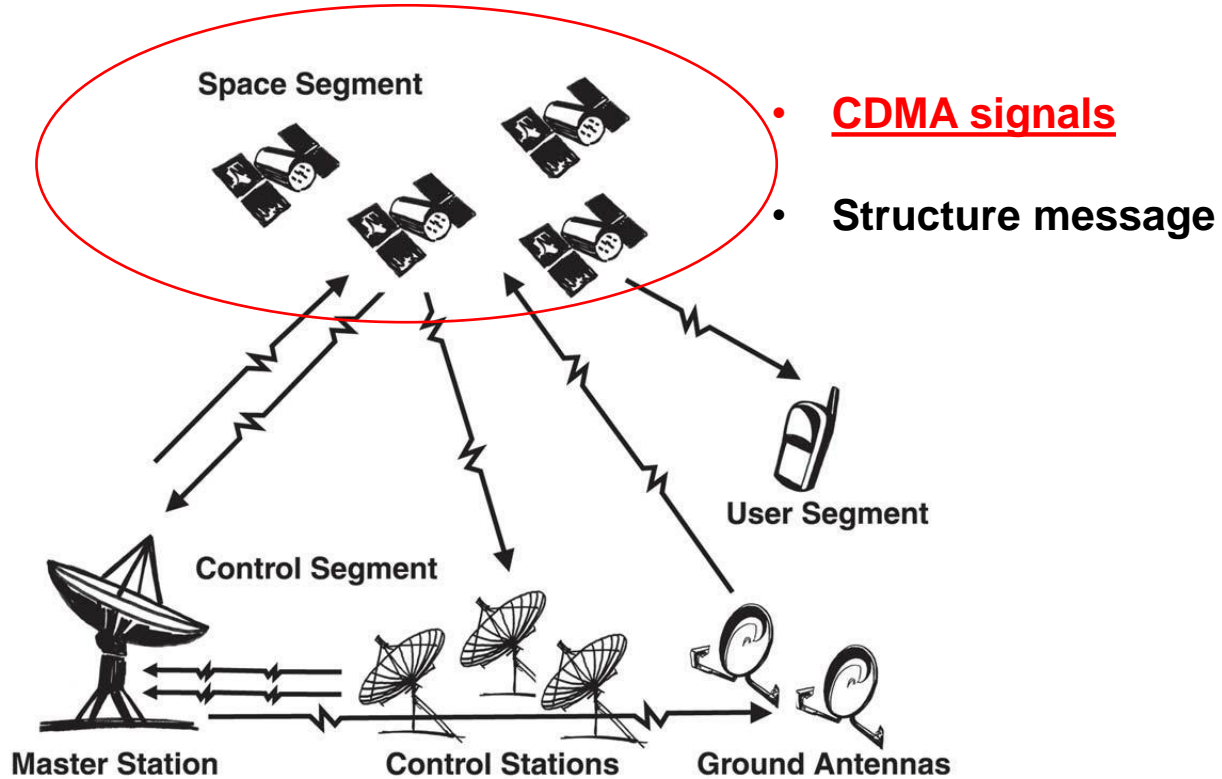
GNSS is 3 Segments system



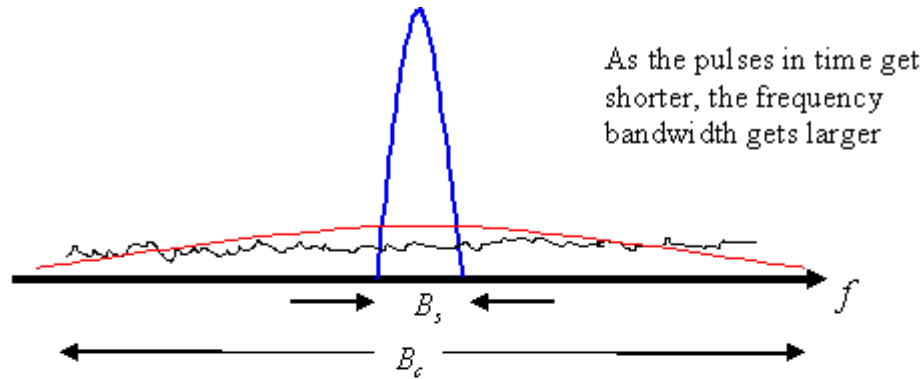
Positioning



GNSS is 3 Segments system



CDMA signal:

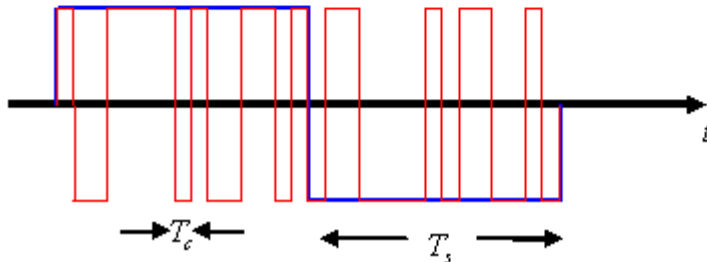


If at the receiver you know the PRN:

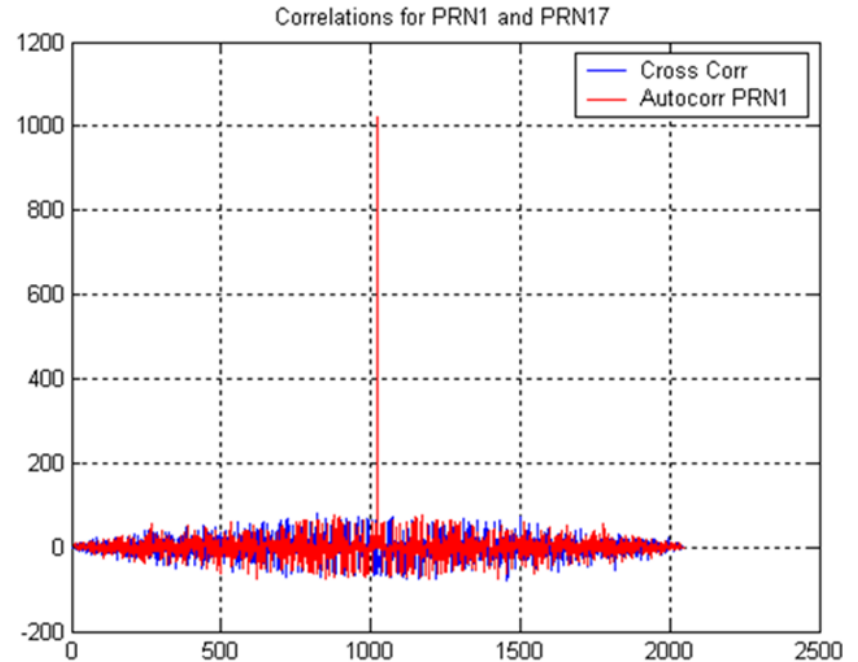
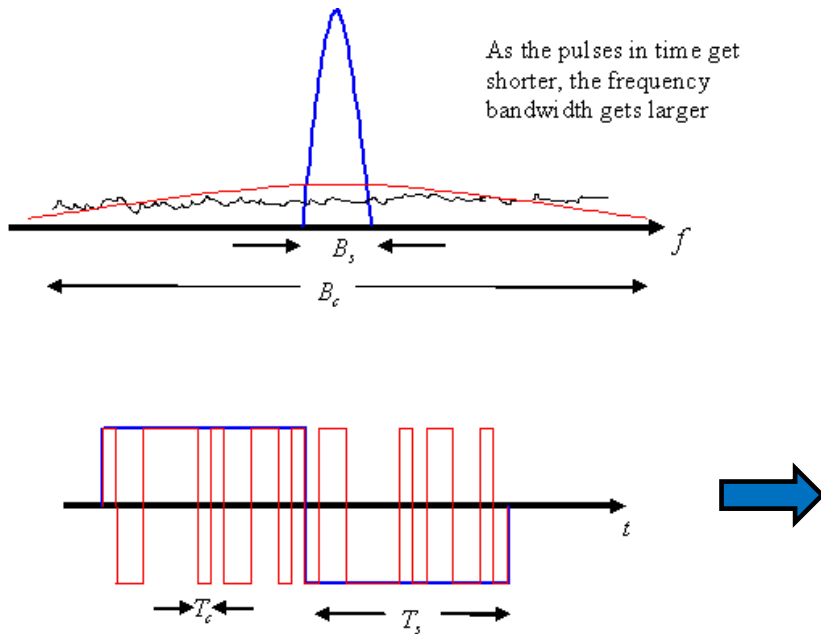
- Robust against narrowband interference
- Less Intra-system Interference



Pseudo Random Noise (PRN) sequence

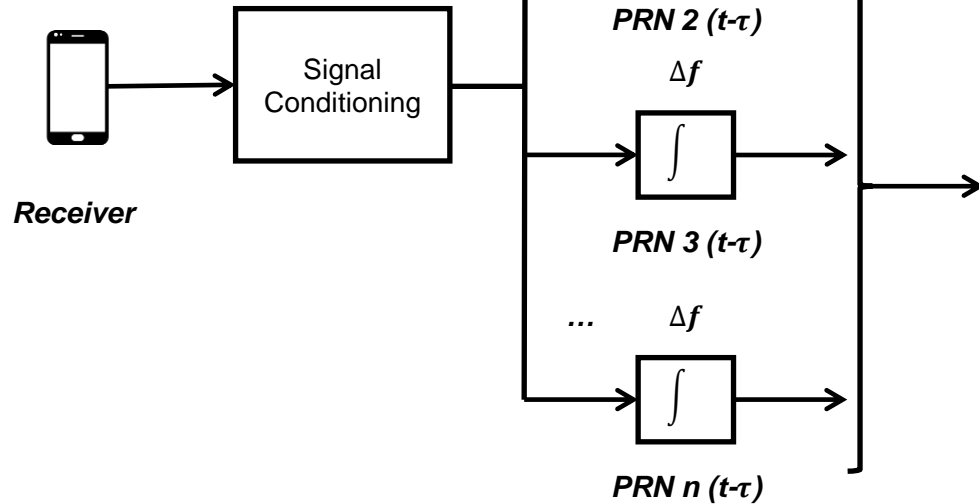


PRN code:

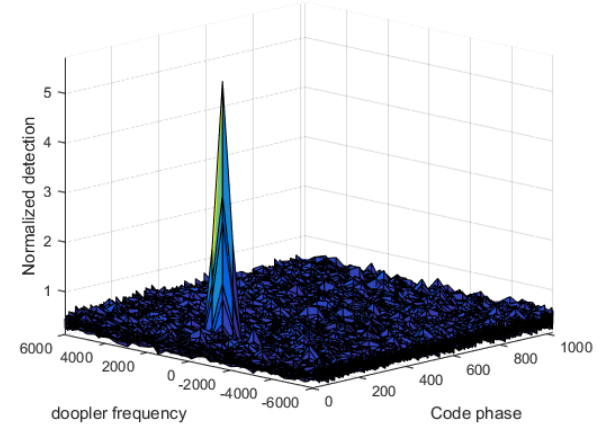


Introduction & Background

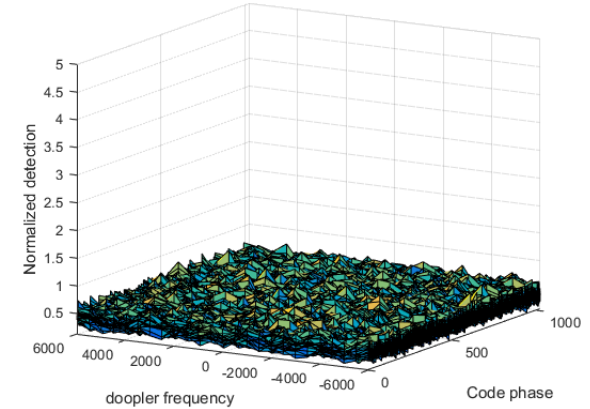
PRN code:



Acquisition Stage GPS L1 C/A



Acquisition Stage GPS L1 C/A



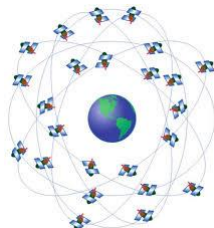
Introduction & Background

Same modulation?

30 Satellites per constellation

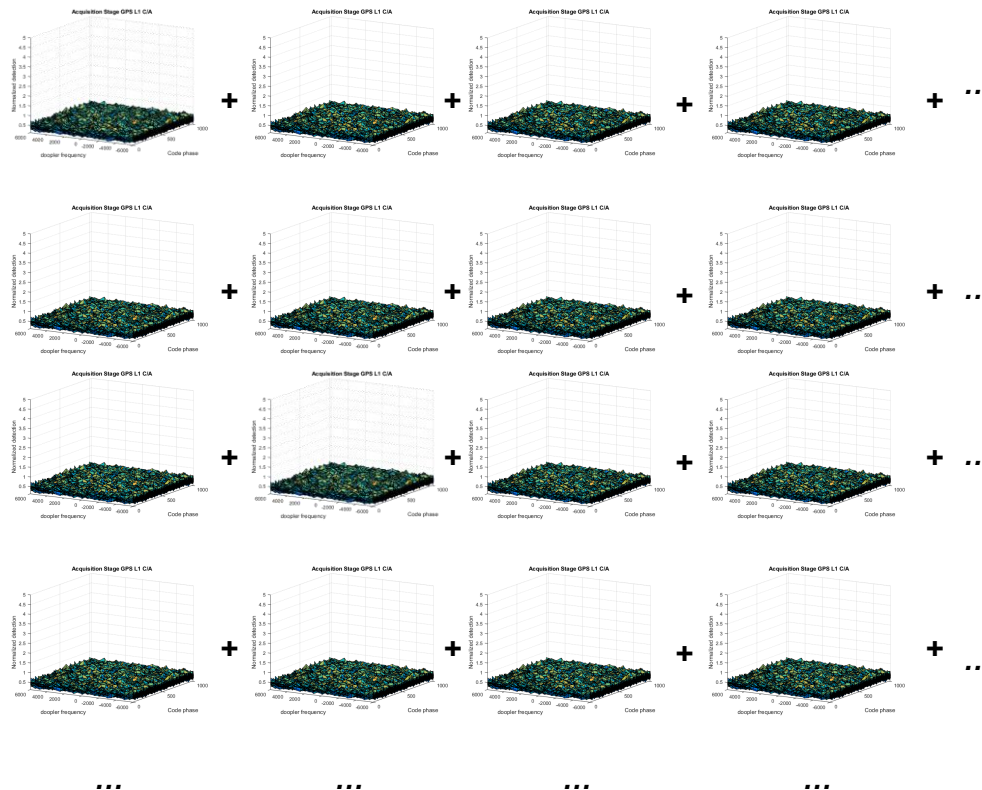


4 Global constellation



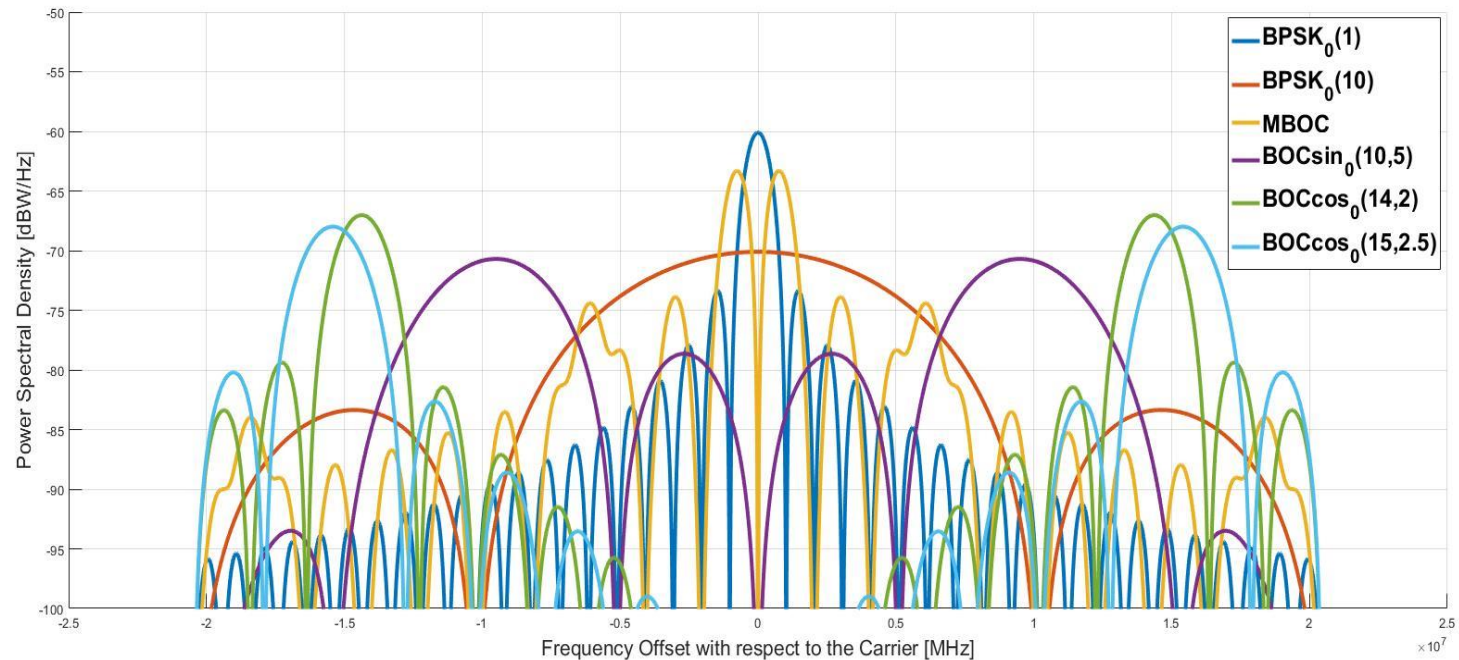
6/7 Signal per band

Number of PRNs?

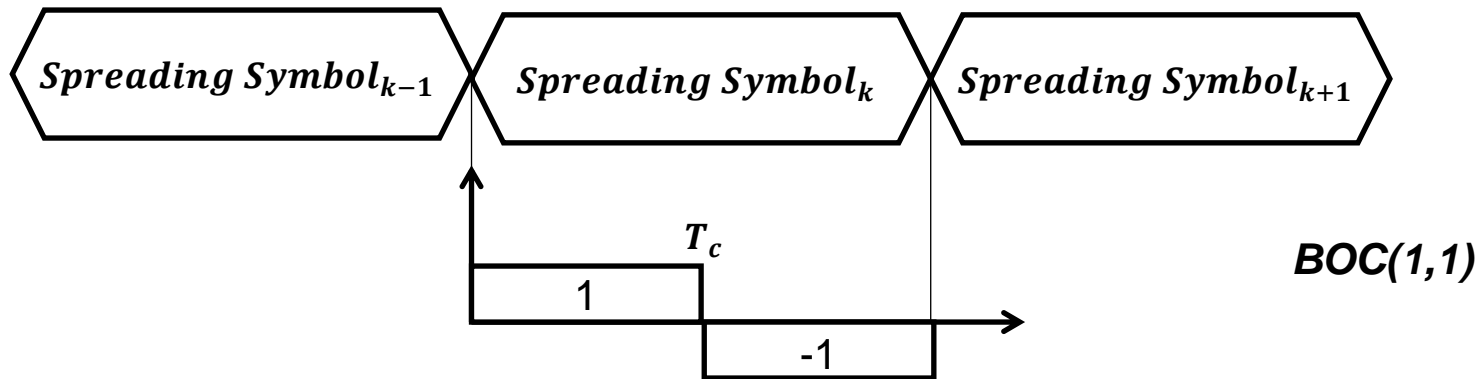
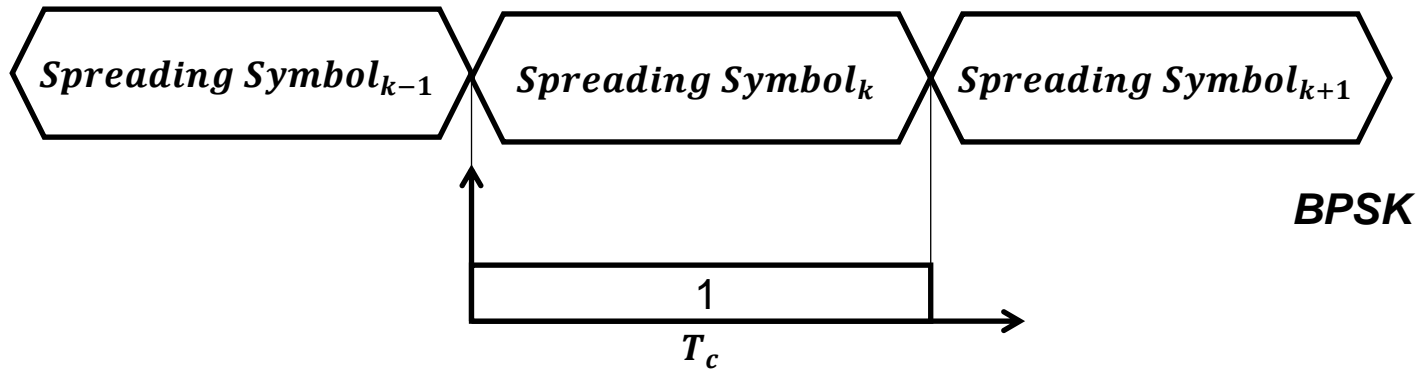


Same modulation?

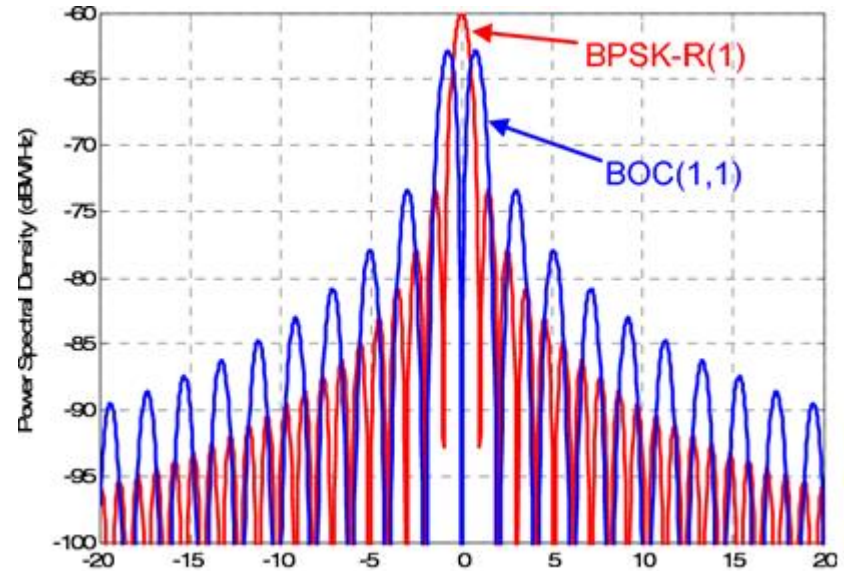
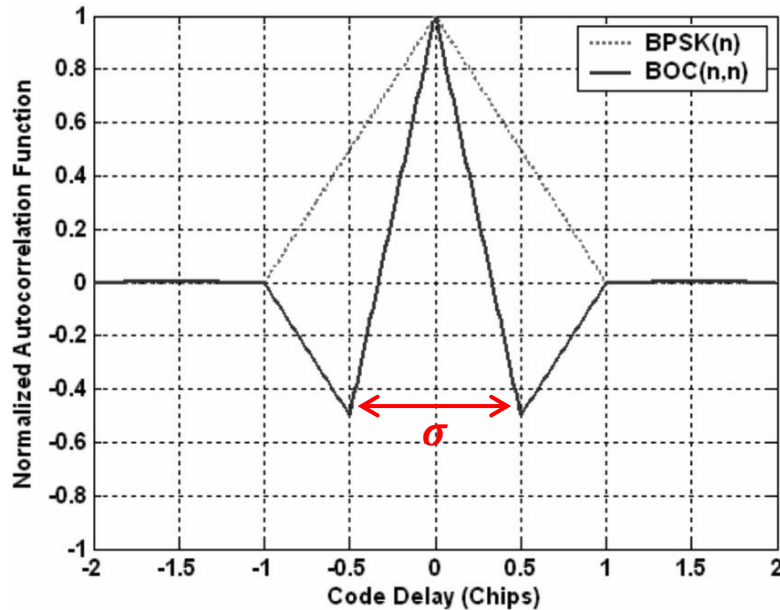
Current L1 bandwidth spectral occupation



Spreading modulation / CDMA signal:



Spreading modulation / CDMA signal:



$$\sigma \propto 1/\text{precision}$$

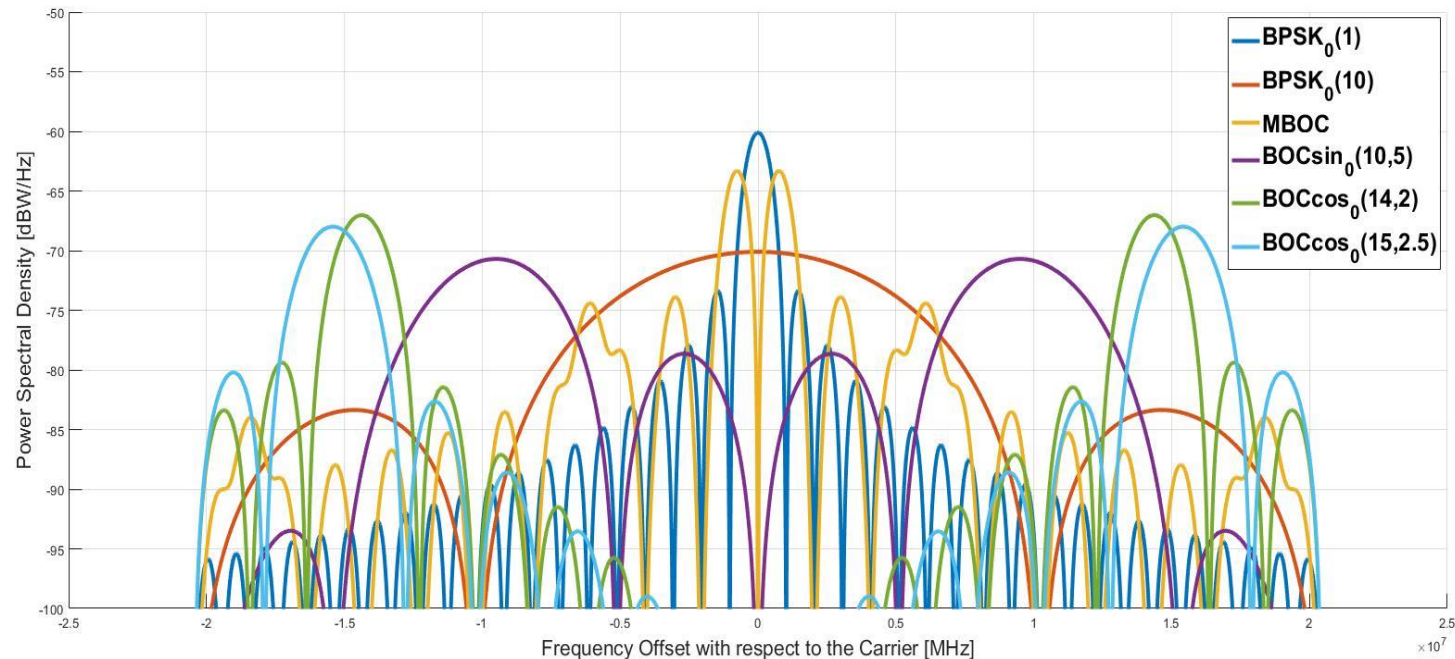
GPS C/A

$$\Delta t = 0.5 \text{ chip} = 9.775171 \cdot 10^{-7}$$

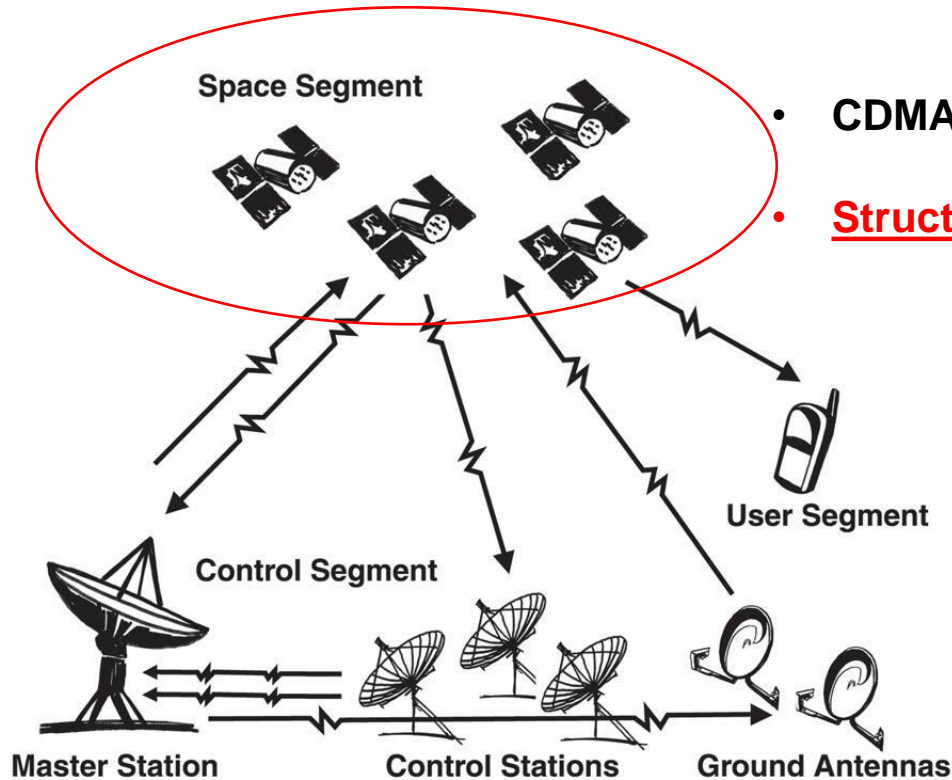
$$\Delta D = (9.775171 \cdot 10^{-7}) * 3 \cdot 10^8 = 293,255\text{m}$$

Spreading modulation / CDMA signal: New Signal

Current L1 bandwidth spectral occupation



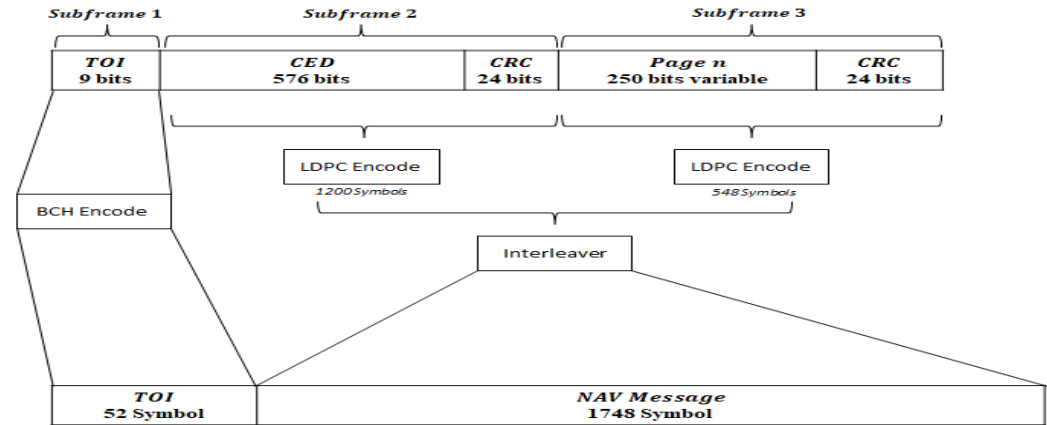
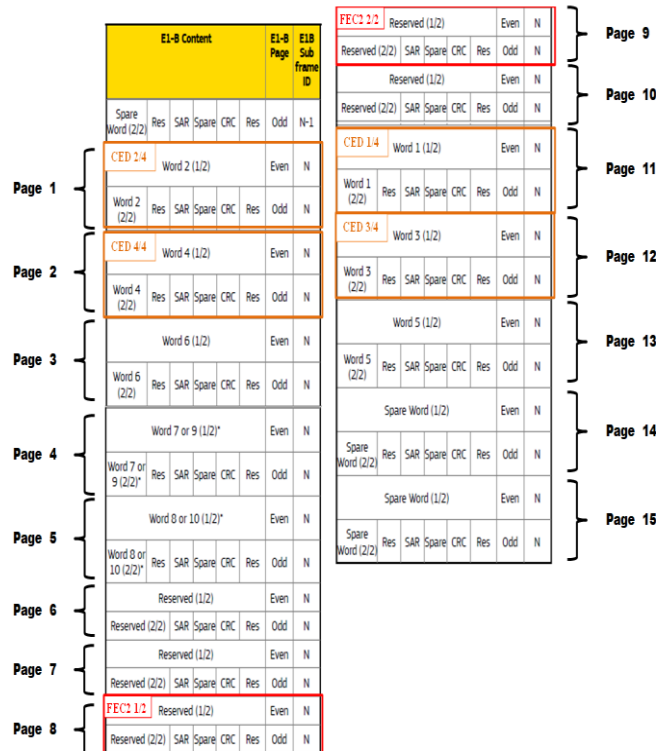
GNSS is 3 Segments system



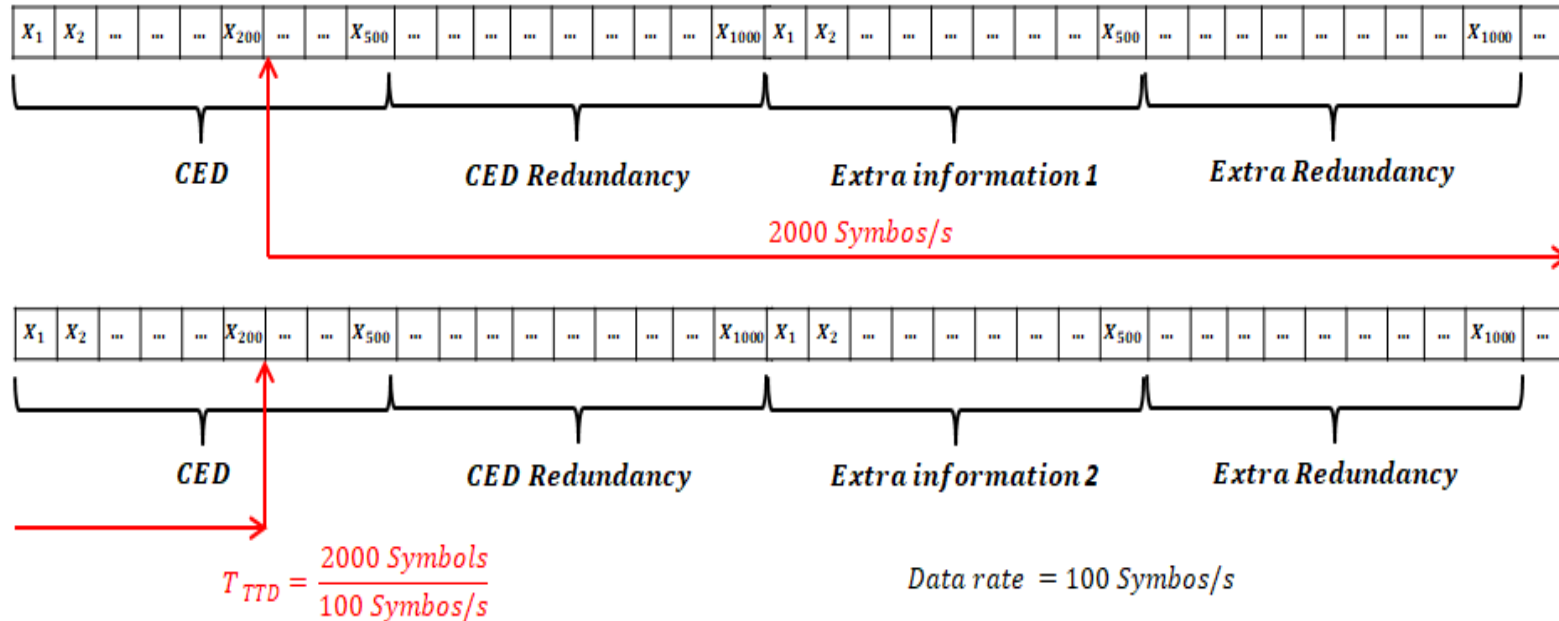
- CDMA signals
- Structure message

Effect of each satellite

Structure of the message: CED



Structure of the message: Acquisition problem



Today: We are going to design a new signal

New signal to improve the **TTFF** and the **receiver sensitivity**

- What does improving the TTFF involve?
- What does improving the receiver sensitivity involve?

New signal to improve the **TTFF** and the **receiver sensitivity**

- What does improving the TTFF involve?

$$TTFF = T_{warm-up} + T_{acq} + T_{track} + T_{CED} + T_{PVT}$$

- What does improving the receiver sensitivity involve?
 - Acquisition
 - Tracking
 - Data Demodulation ...

New signal to improve the TTFF and the receiver sensitivity

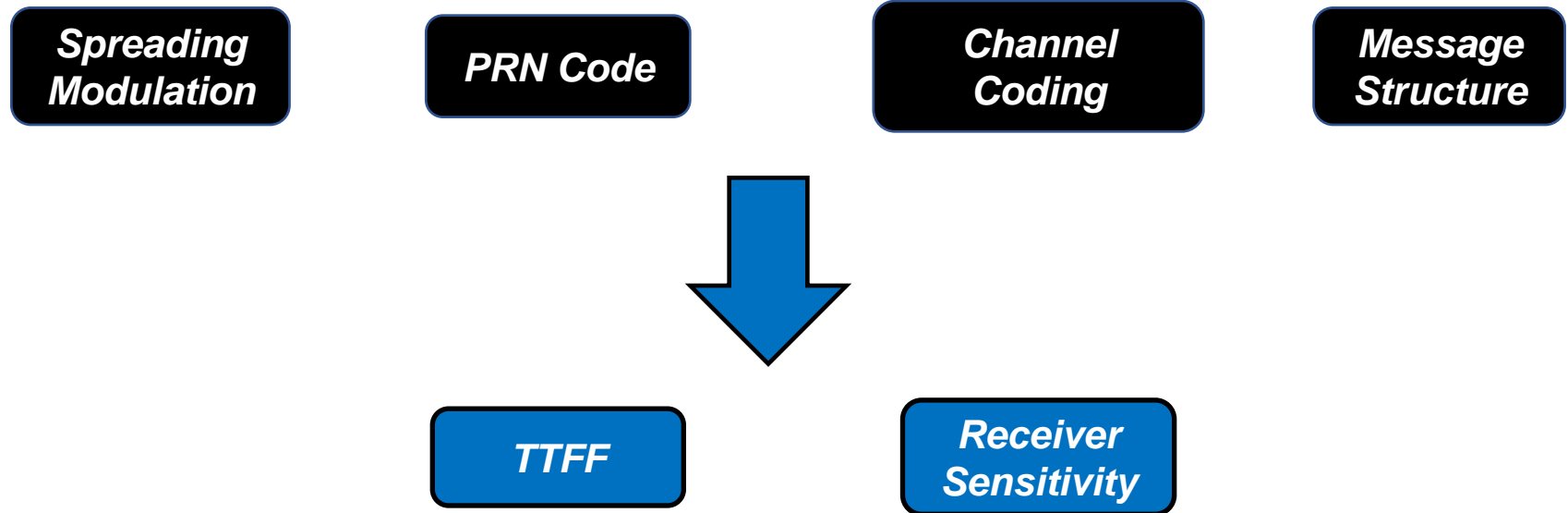
Spreading Modulation

PRN Code

Channel Coding

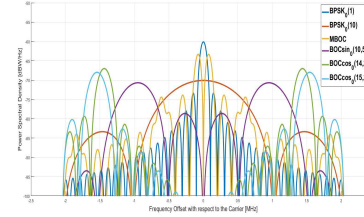
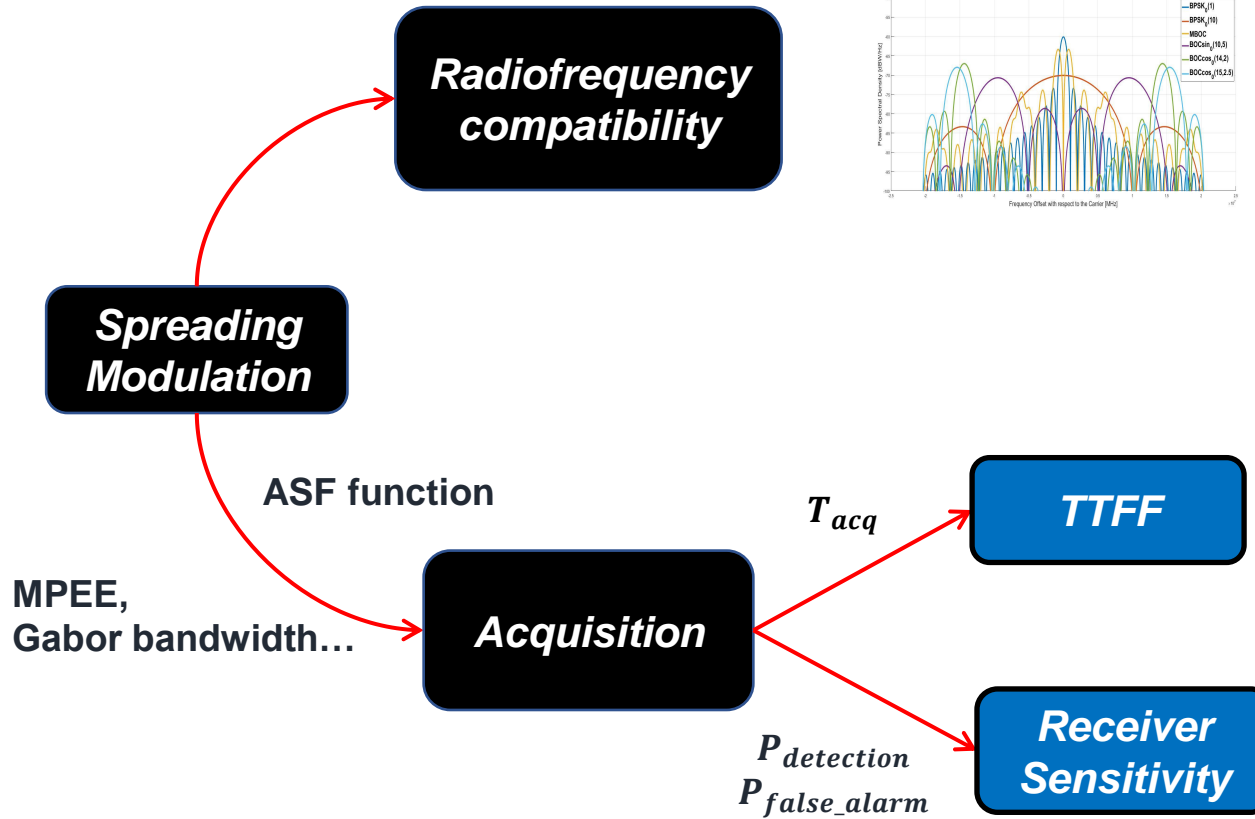
Message Structure

New signal to improve the TTFF and the receiver sensitivity



- Introduction & background
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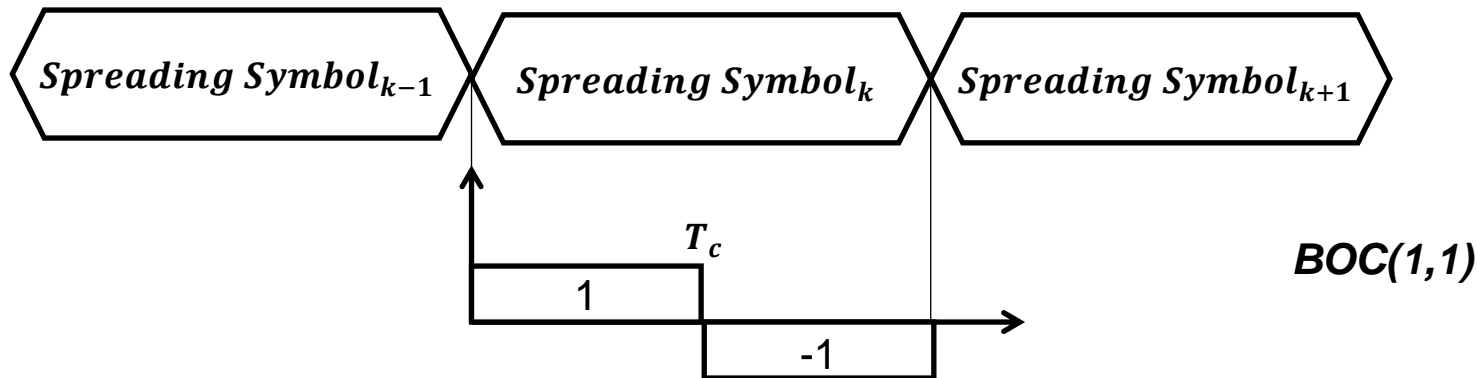
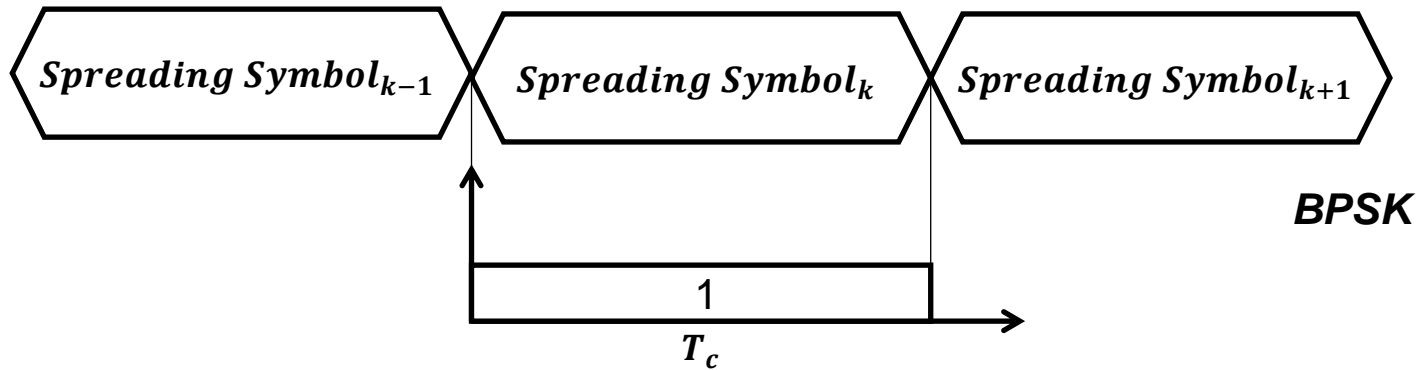
Design new modulation



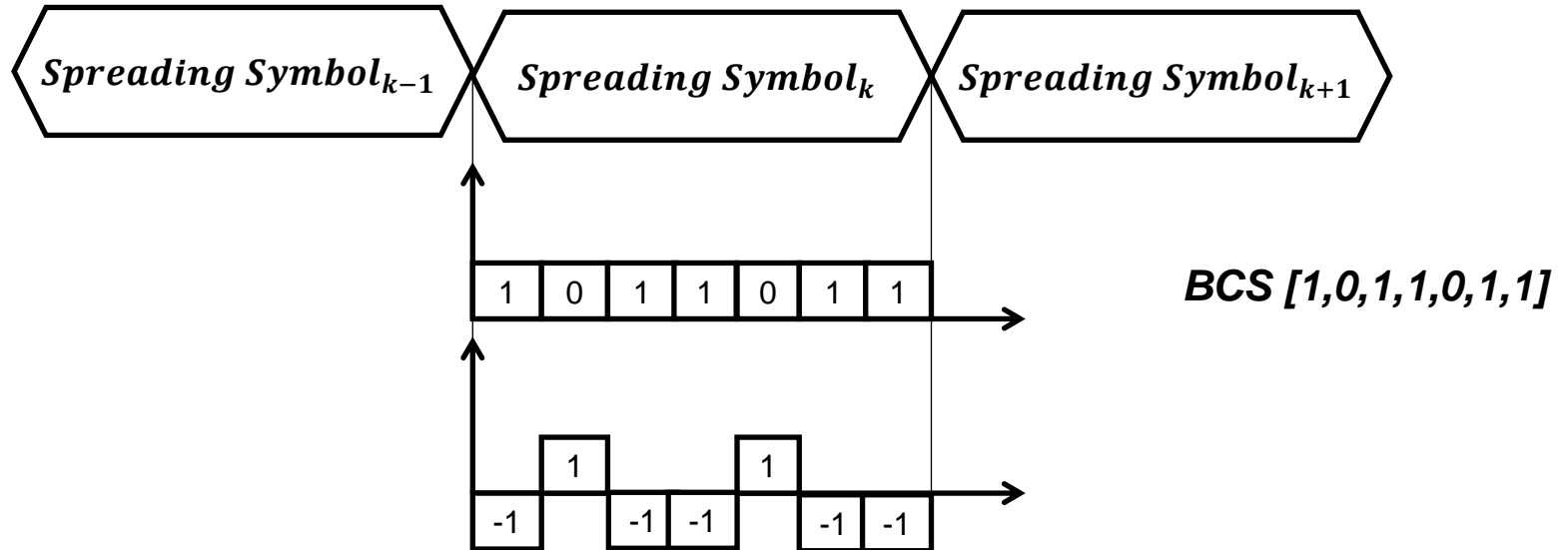
- Spreading Modulation Criteria for Design

Figure of Merit	Criteria
Radio Frequency Compatibility	SSC
Correlation Properties	ACF
Resistance Against Multipath	MPEE
Ranging Performance	Gabor bandwidth
Anti-Jamming Capability	Demodulation & anti-jamming of narrowband Code tracking & anti-jamming of narrowband Demodulation & anti-jamming of matched spectrum Code tracking & anti-jamming of matched spectrum

- Standard spreading modulations:



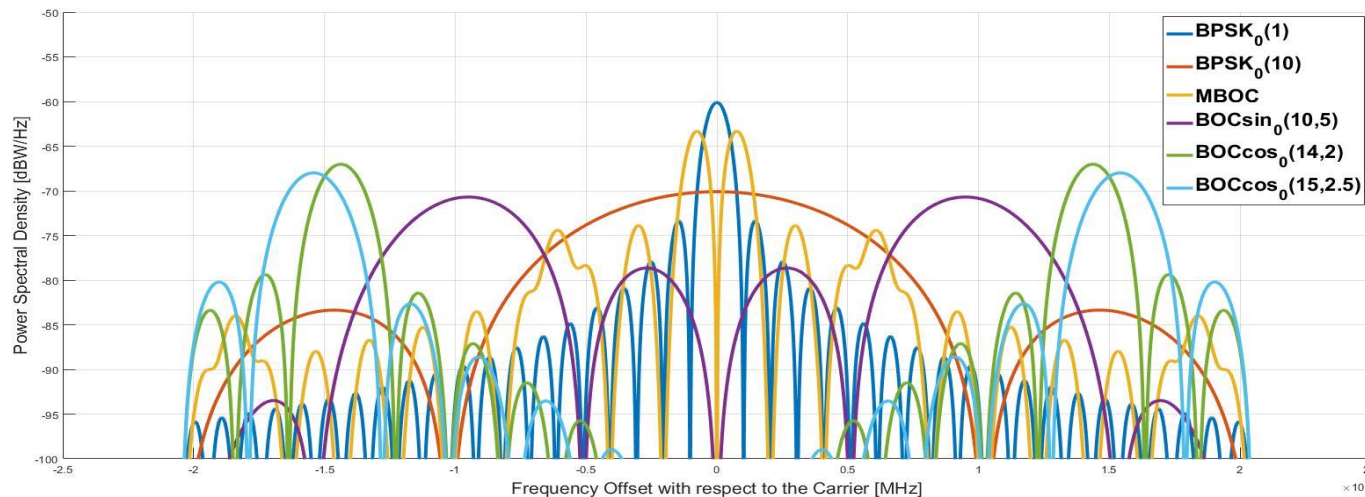
- Binary Coded Symbol (BCS)
 - Spreading modulation candidate



- Spreading modulation candidates

Already proposed candidates		Proposed candidates	
BOCcos(0.5,0.5)	BOCsin(4, 1),	BCS[-1,1](0.5)	BCS[-1,-1, -1, 1, 1](1)
BOCsin(0.5,0.5)	BOCcos(4,1),	BCS[-1,1,-1](0.5)	BCS[-1,1,-1](1)
BOCsin(4,0.5)	BOCsin(6.5,0.5)	BCS[-1,-1,-1,1,1](0.5)	BCS[-1,-1,-1,1,-1](1)
BOCcos(4,0.5)	BOCcos(6.5,0.5)		

Current L1 bandwidth spectral occupation



- Evaluation of the spreading modulation candidates
 - Radio frequency compatibility

More interference



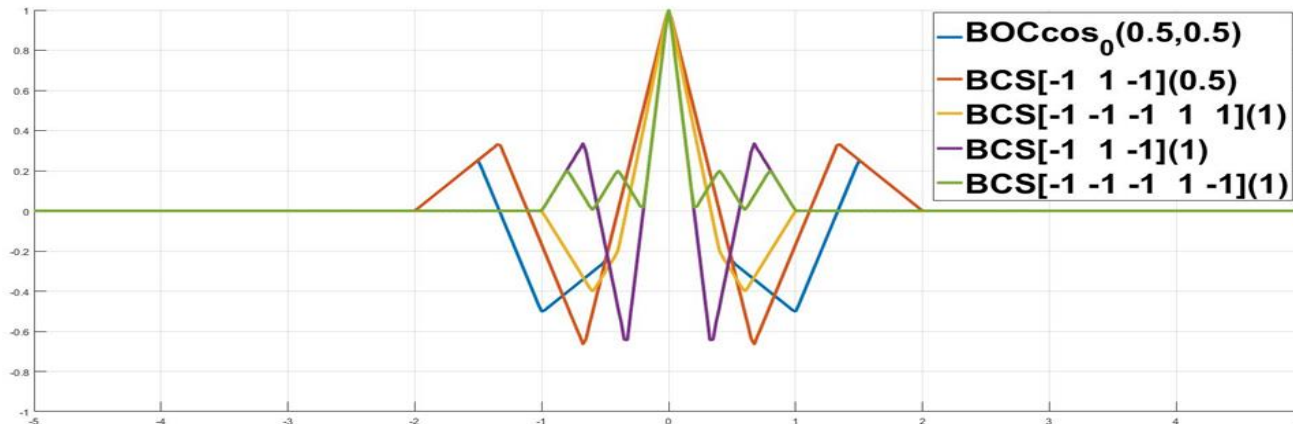
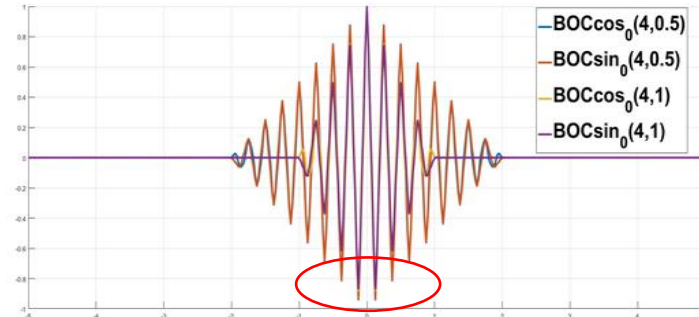
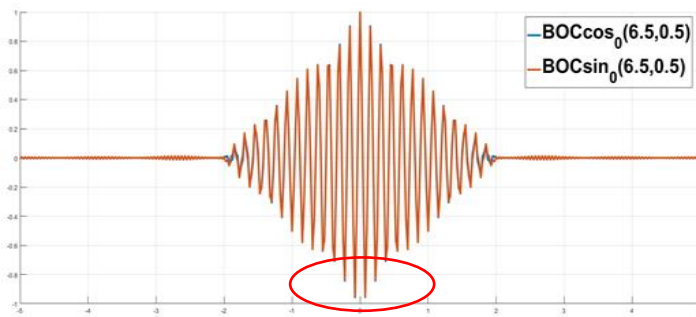
Less interference

Candidates

	SSC Coefficients					
BOCcos ₀ (6.5,0.5)	-88.43	-78.27	-79.09	-77.49	-90.91	-90.29
BOCsin ₀ (6.5,0.5)	-85.40	-77.79	-78.46	-77.85	-94.23	-92.64
BOCcos ₀ (4,0.5)	-88.96	-73.54	-87.47	-80.91	-96.51	-94.08
BOCsin ₀ (4,0.5)	-82.93	-73.26	-82.99	-81.20	-95.06	-94.09
BOCcos ₀ (4,1)	-85.95	-73.66	-84.46	-80.46	-93.48	-93.83
BOCsin ₀ (4,1)	-79.92	-73.11	-79.98	-81.00	-92.04	-93.84
BOCcos ₀ (0.5,0.5)	-66.12	-70.48	-65.27	-83.92	-92.96	-93.57
BOCsin ₀ (0.5,0.5)	-63.11	-70.32	-66.52	-86.13	-95.17	-95.79
BCS[-1 1](0.5)	-63.11	-70.32	-66.52	-86.13	-95.17	-95.79
BCS[-1 1 -1](0.5)	-66.75	-70.48	-64.86	-83.92	-92.94	-93.56
BCS[-1 -1 -1 1 1](0.5)	-63.09	-70.32	-66.57	-86.13	-95.17	-95.79
BCS[-1 -1 -1 1 1](1)	-67.39	-70.56	-65.50	-83.12	-91.68	-92.80
BCS[-1 1 -1](1)	-71.40	-70.89	-68.98	-80.90	-88.80	-91.90
BCS[-1 -1 -1 1 -1](1)	-66.11	-70.89	-69.37	-80.90	-91.31	-94.60
	BPSK ₀ (1)	BPSK ₀ (10)	MBOC	BOCsin ₀ (10,5)	BOCcos ₀ (14,2)	BOCcos ₀ (15,2.5)

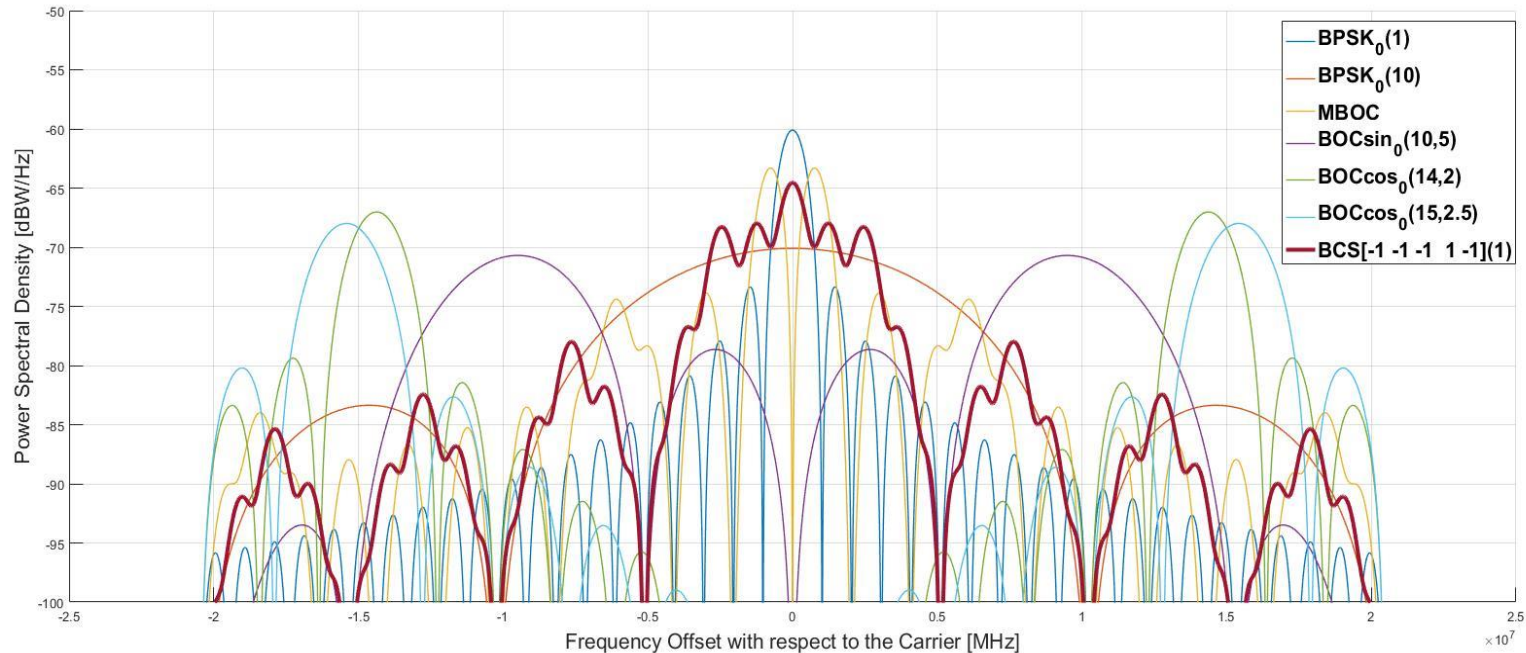
Current signals

- Evaluation of the spreading modulation candidates
 - Correlation properties



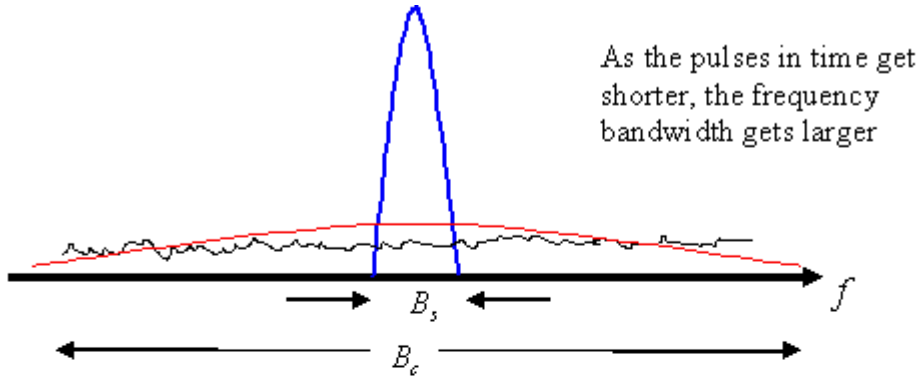
- Evaluation of the spreading modulation candidates

BCS[-1,-1,-1,1,-1](1)



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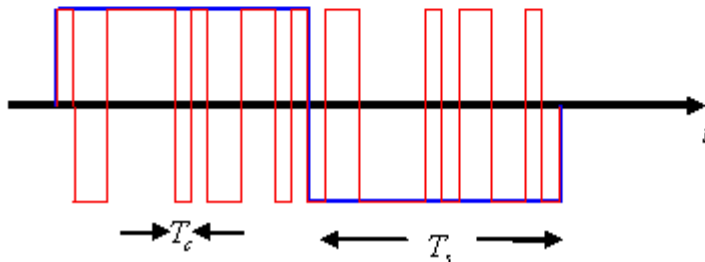
CDMA signal:



If at the receiver you know the PRN:

- Robust against narrowband interference
- Less Intra-system Interference

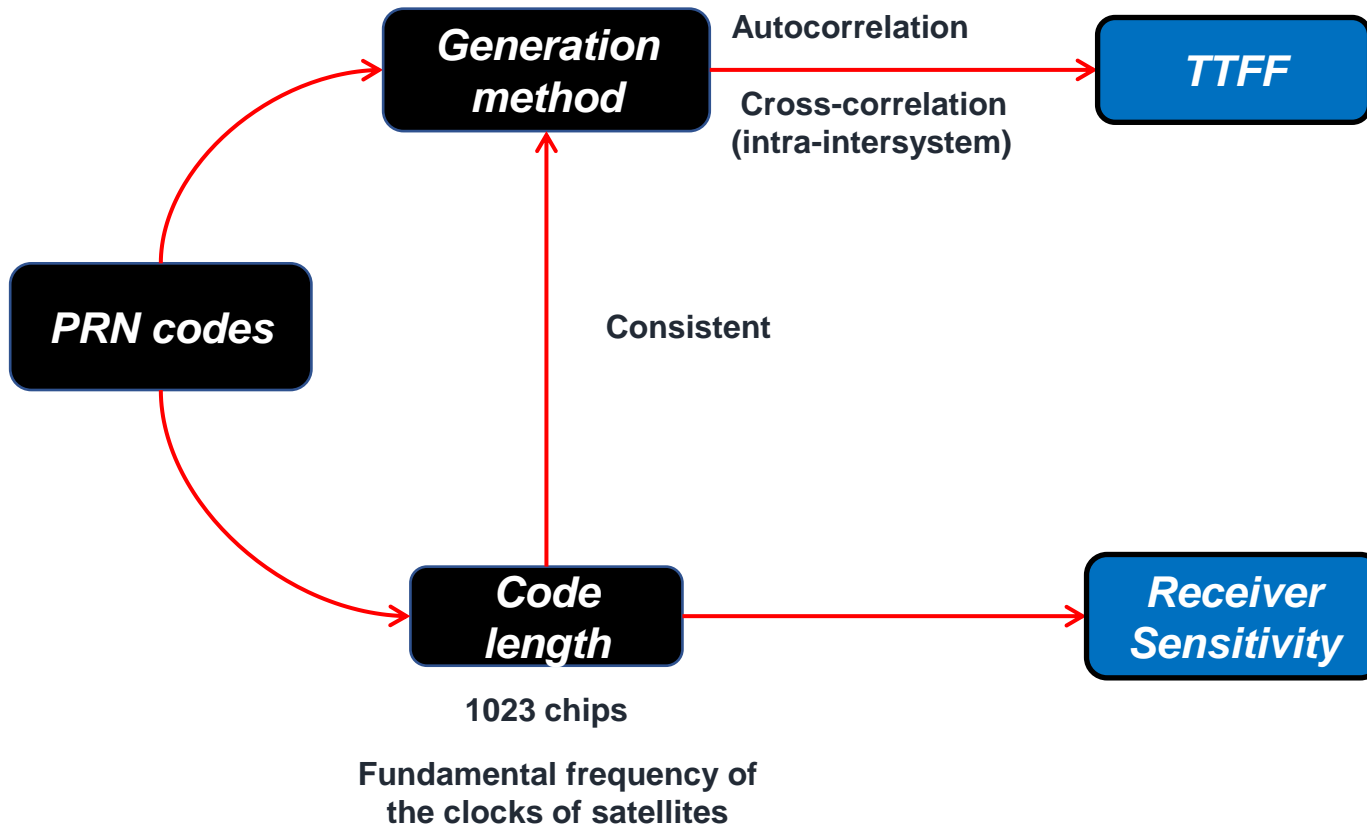
Pseudo Random Noise (PRN) sequence



GPS: Gold codes

- Good Autocorrelation
- Good Cross-correlation

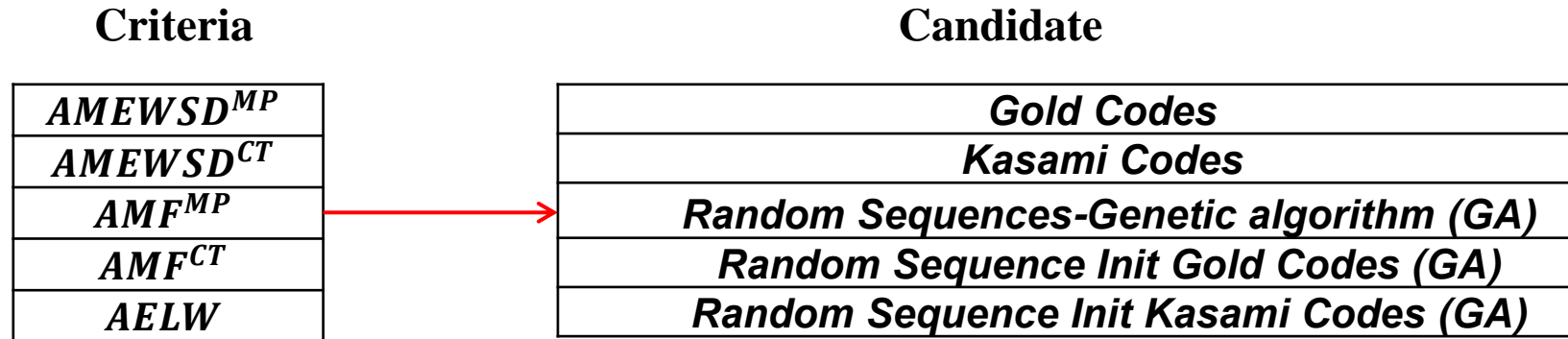
Design new PRN codes



- PRN codes criteria for design

Criteria	Equations
<p style="text-align: center;">Acquisition Criterion</p>	$MEWSD^{MP} = \text{mean} \left(\sum_{n_{\text{offs}}} \sum_{\substack{l=1 \\ ACF^e(l, f_{\text{offs}}) > \Phi_{\text{min}}}}^{N-1} (ACF^e(l, f_{\text{offs}}) - \Phi_{\text{min}})^2 \right)$ $MEWSD^{CT}_{i,j} = \text{mean} \left(\sum_{n_{\text{offs}}} \sum_{\substack{l=1 \\ CC^e(l, f_{\text{offs}}) > \Phi_{\text{min}}}}^{N-1} (CC^e(l, f_{\text{offs}}) - \Phi_{\text{min}})^2 \right)$
<p style="text-align: center;">Tracking Criterion</p>	$MF_i^{MP} = \frac{1}{n_{\text{offs}}} \left(\sum_{n_{\text{offs}}} \left(\sum_{l=1,2,N-2,N-1} (AC_i^e(l, f_{\text{offs}}))^2 \right) \right)$ $MF_{i,j}^{CT} = \frac{1}{n_{\text{offs}}} \left(\sum_{n_{\text{offs}}} \left(\sum_{l=0}^{N-1} (CC_{i,j}^e(l, f_{\text{offs}}))^2 \right) \right)$
<p style="text-align: center;">Robustness Against Narrow-Band Interferences Criterion</p>	$ELW = 10 \log \left(\frac{1}{n} \sum_{\substack{k=-\frac{n}{2} \\ A_k > \sqrt{n}}}^{\frac{n}{2}} (A_k - \sqrt{n})^2 \right)$

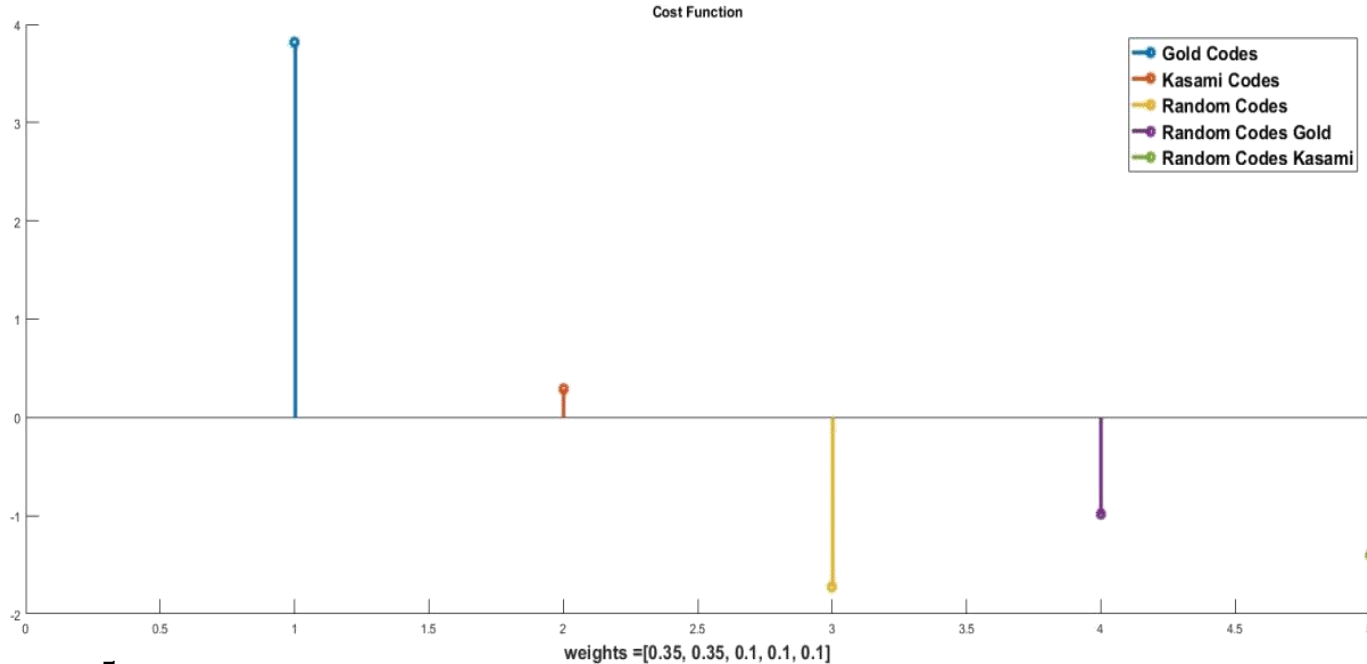
- PRN codes assessment



$$R_i = \sum_{j=1}^5 -w_j \frac{\overline{cv_j} + cv_{i,j}}{\overline{cv_j}} \text{ for } i = 1, 2, \dots, K$$

$$\text{Weight} = [0.2, 0.2, 0.2, 0.2, 0.2]$$

- PRN codes assessment

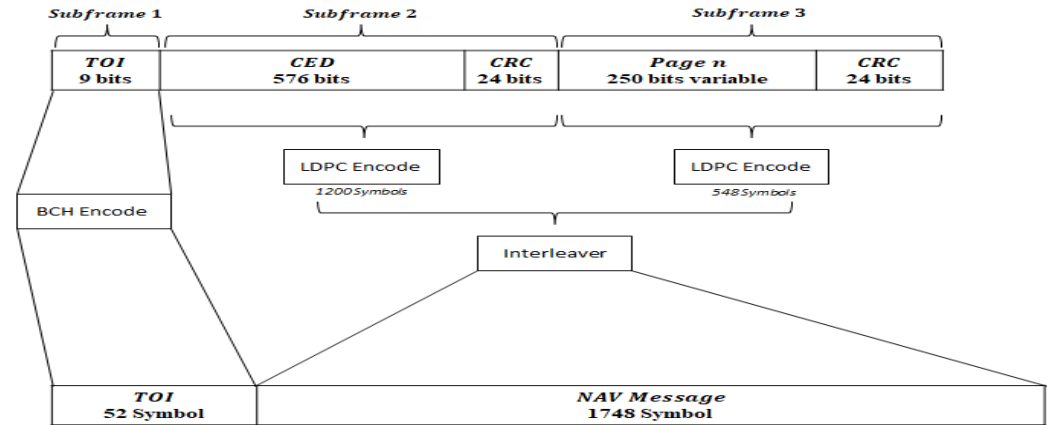
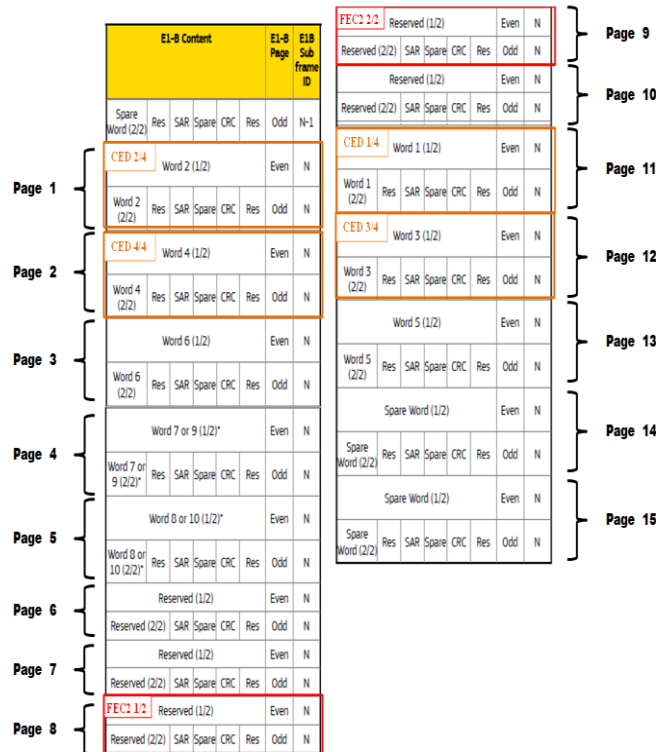


$$R_i = \sum_{j=1}^5 -w_j \frac{\overline{cv_j} + cv_{i,j}}{\overline{cv_j}} \text{ for } i = 1, 2, \dots, K$$

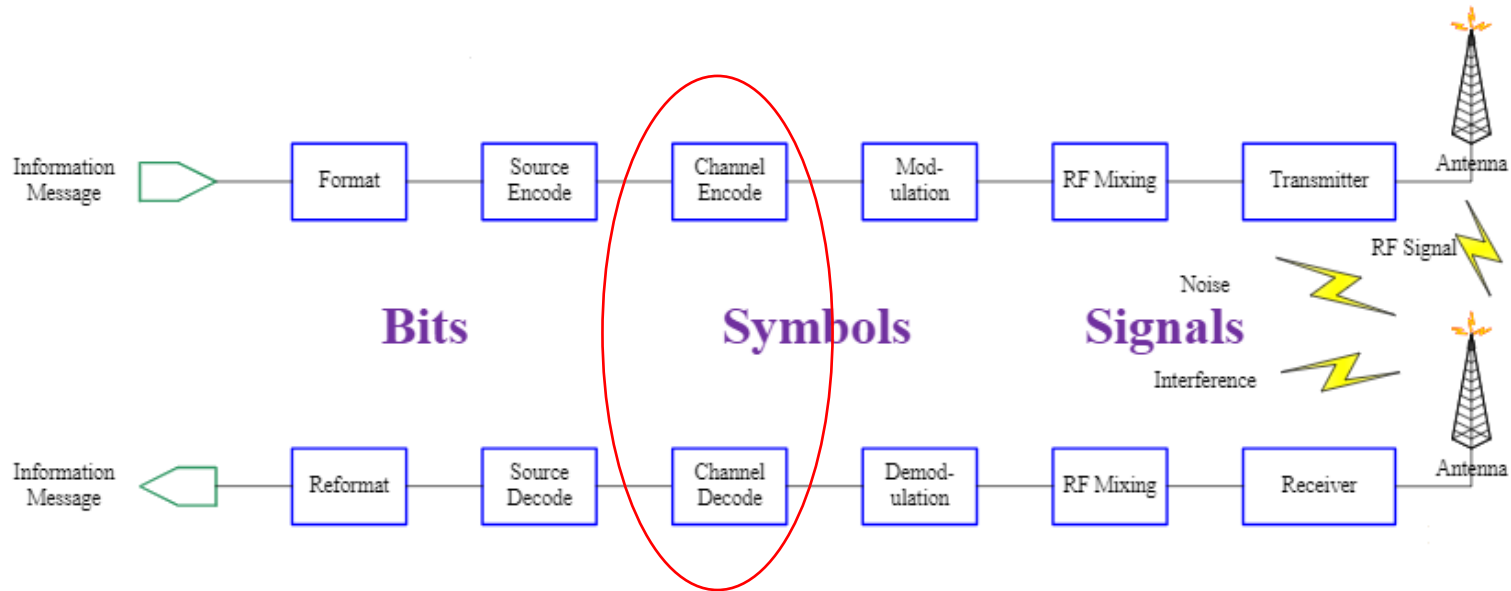
$$\text{Weight} = [0.35, 0.35, 0.1, 0.1, 0.1]$$

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Structure of the message: CED



Introduction to channel coding:



Extra data to enhance the reliability of a communication system

Introduction to channel coding:

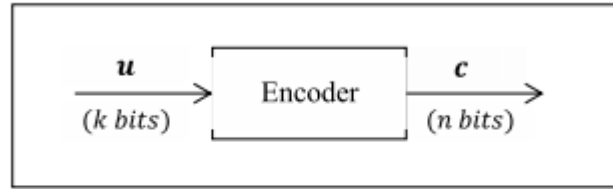


Figure 31 : Classical encoder representation

$$u = (u_0, u_1, \dots, u_{k-1})$$

$$c = (c_0, c_1, \dots, c_{n-1})$$

Generator Matrix G_β :

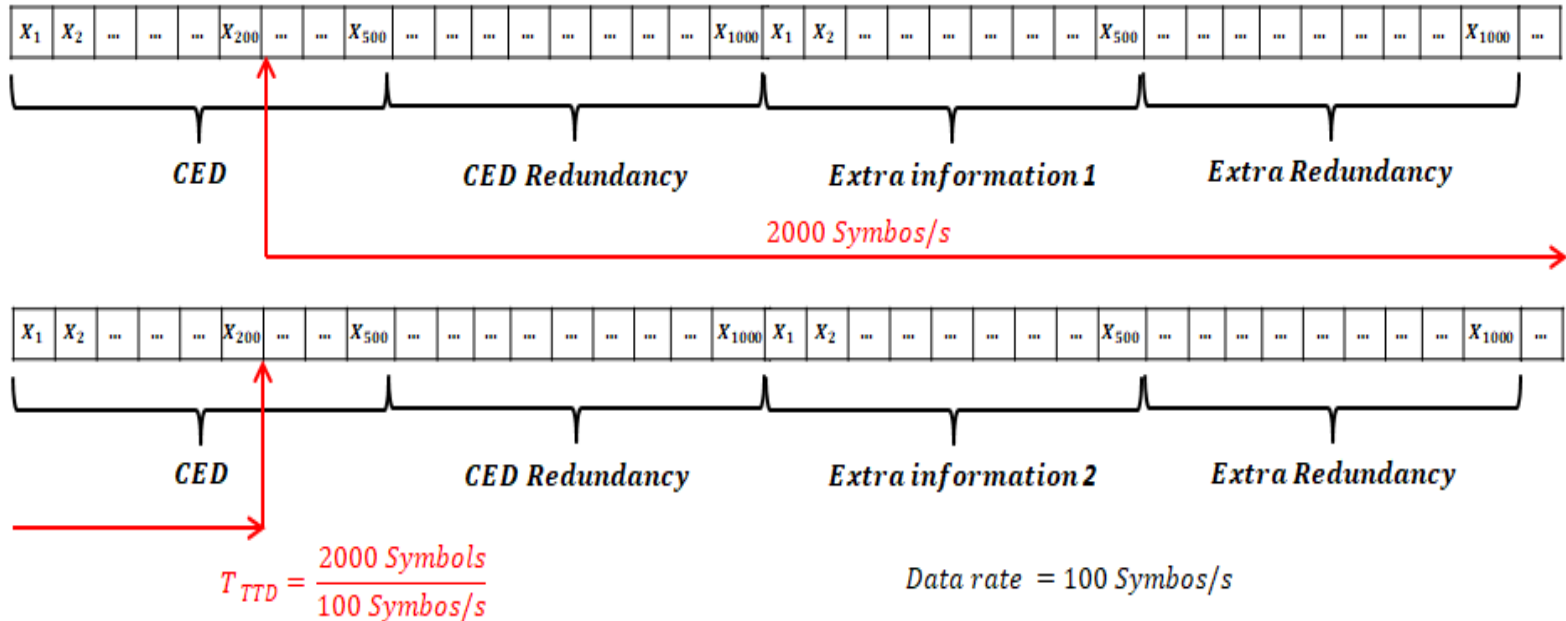
$$c = u \cdot G_\beta$$

$$G_\beta \cdot H_\beta^T = 0$$

Parity check matrix H_β :

$$c \cdot H_\beta^T = 0$$

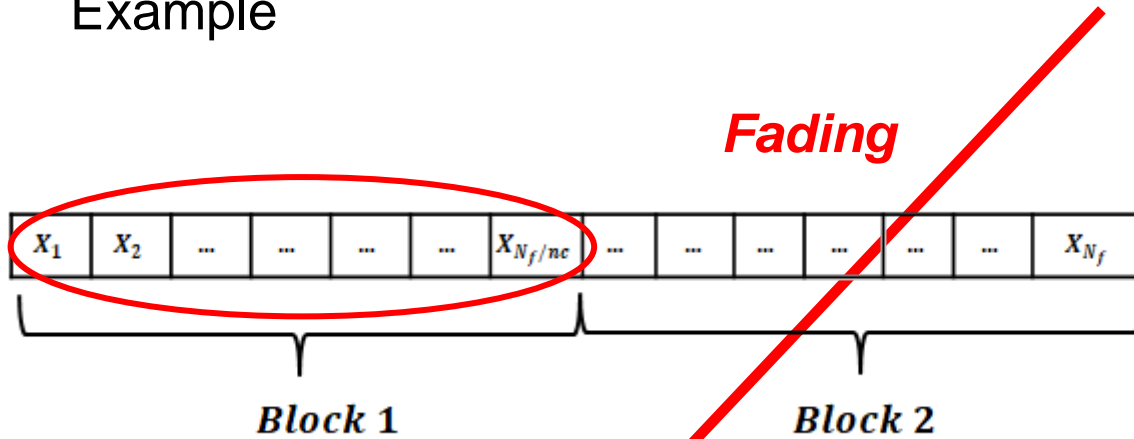
Structure of the message: Acquisition



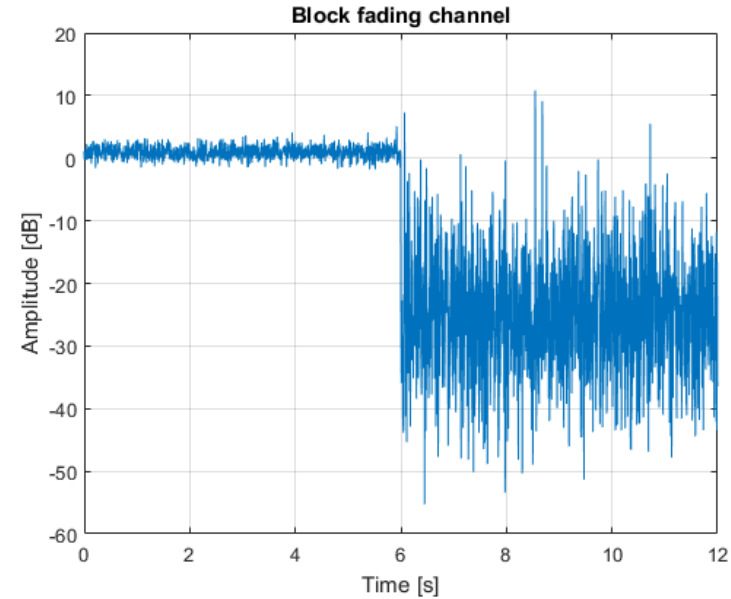
Find a co-design where the CED can be decoded even if some part of the message has not been received.

Block fading with erasure channel model

Example



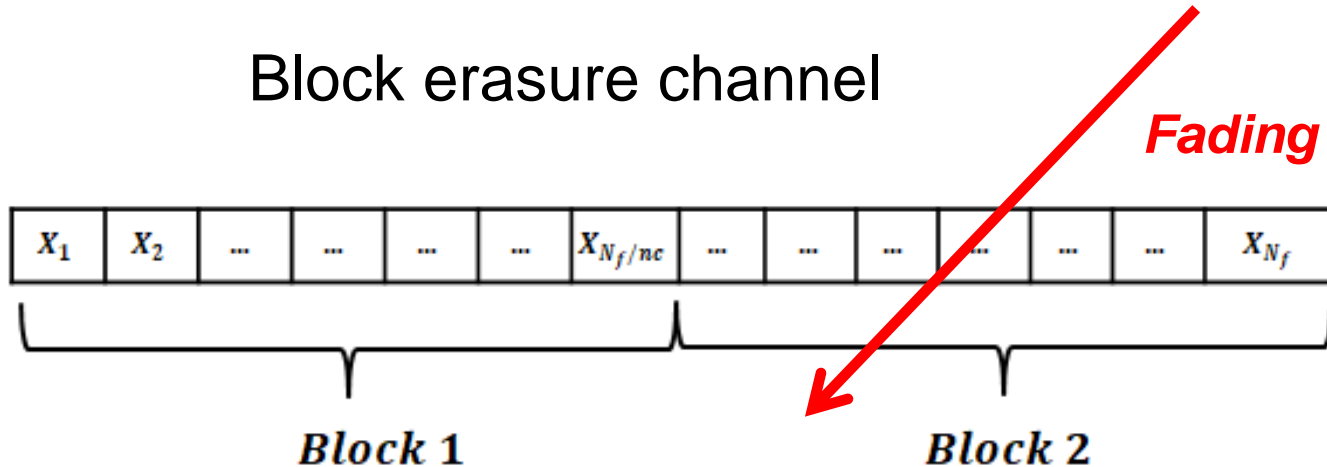
We recover the information



Amplitude of block fading channel

Block fading with erasure channel model

Block erasure channel

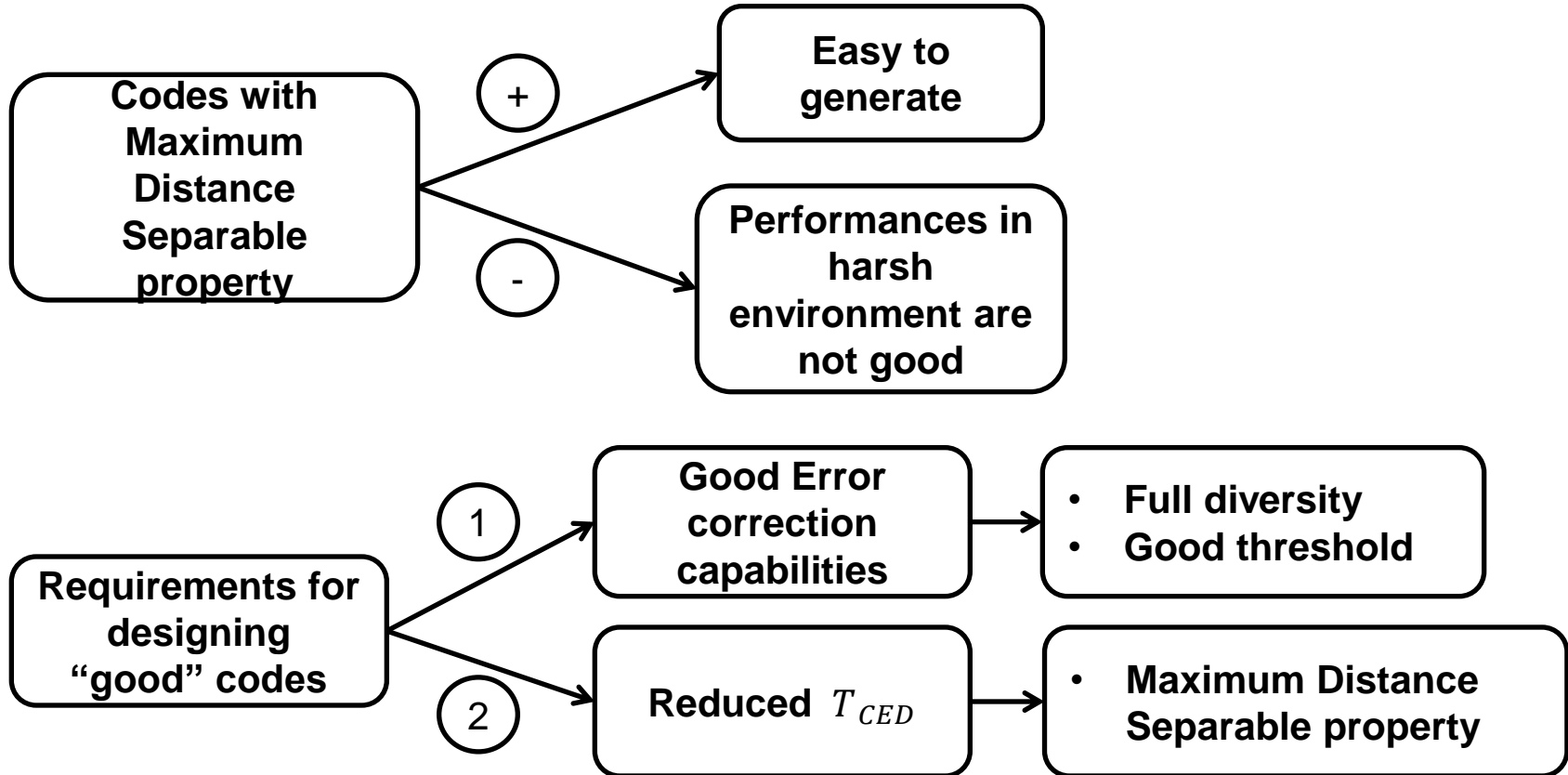


Fading = not have already received the information

but we are able to retrieve the information with the first part

Maximum distance separable (MDS) property

Block fading channel model



- Lowest Density-Maximum Distance Separable (LD-MDS) codes
- Maximum Distance Separable (MDS) codes
- Regular Root codes
- Protograph Root codes

LD-MDS codes

Example:

$$H_{\beta} = \begin{pmatrix} I & I & I & 0 \\ \beta_1 & \beta_2 & 0 & I \end{pmatrix}$$

← 1200 →

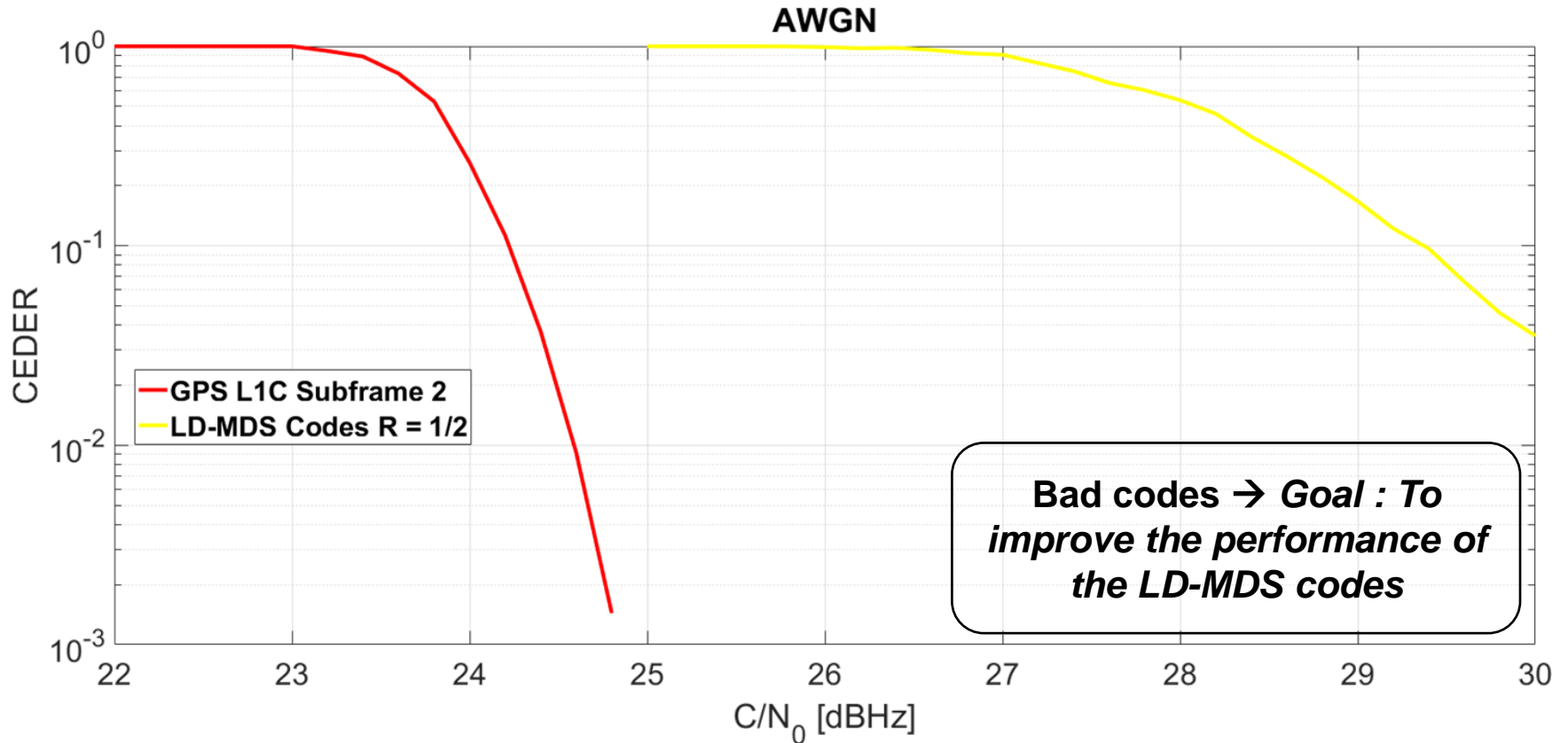
↑ 600 ↓

┌──┬──┬──┬──┐

k1 k2 k3 k4

With any 2 error-free-blocks we retrieve the information → Erasure algorithm
In case of errors with more than 2 blocks → BP Algorithm

LD-MDS codes



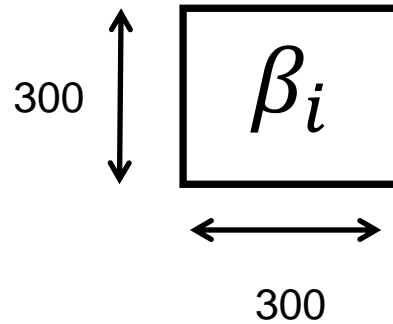
MDS codes

Example:

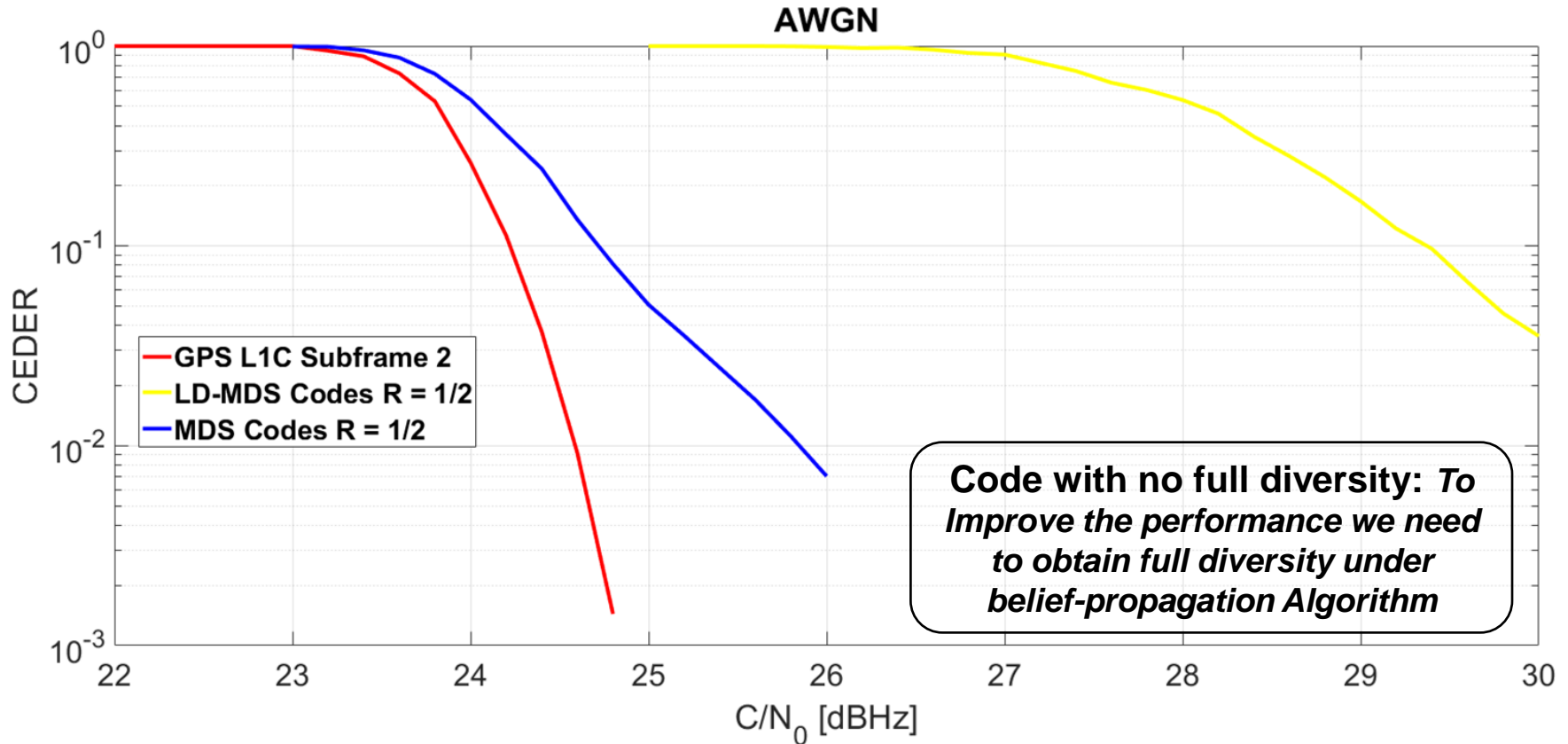
$$H_{\beta} = \begin{pmatrix} \beta'_1 & \beta'_2 & I & 0 \\ \beta_1 & \beta_2 & 0 & I \end{pmatrix}$$

← 1200 →

↑ 600 ↓



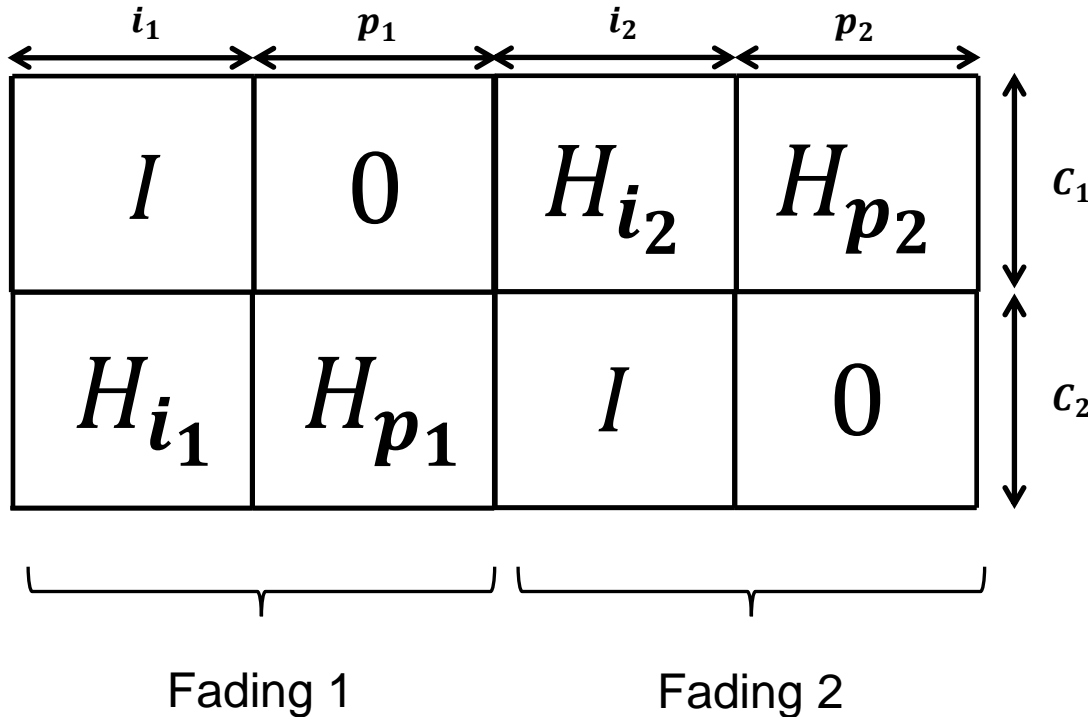
MDS codes



Regular-Root codes

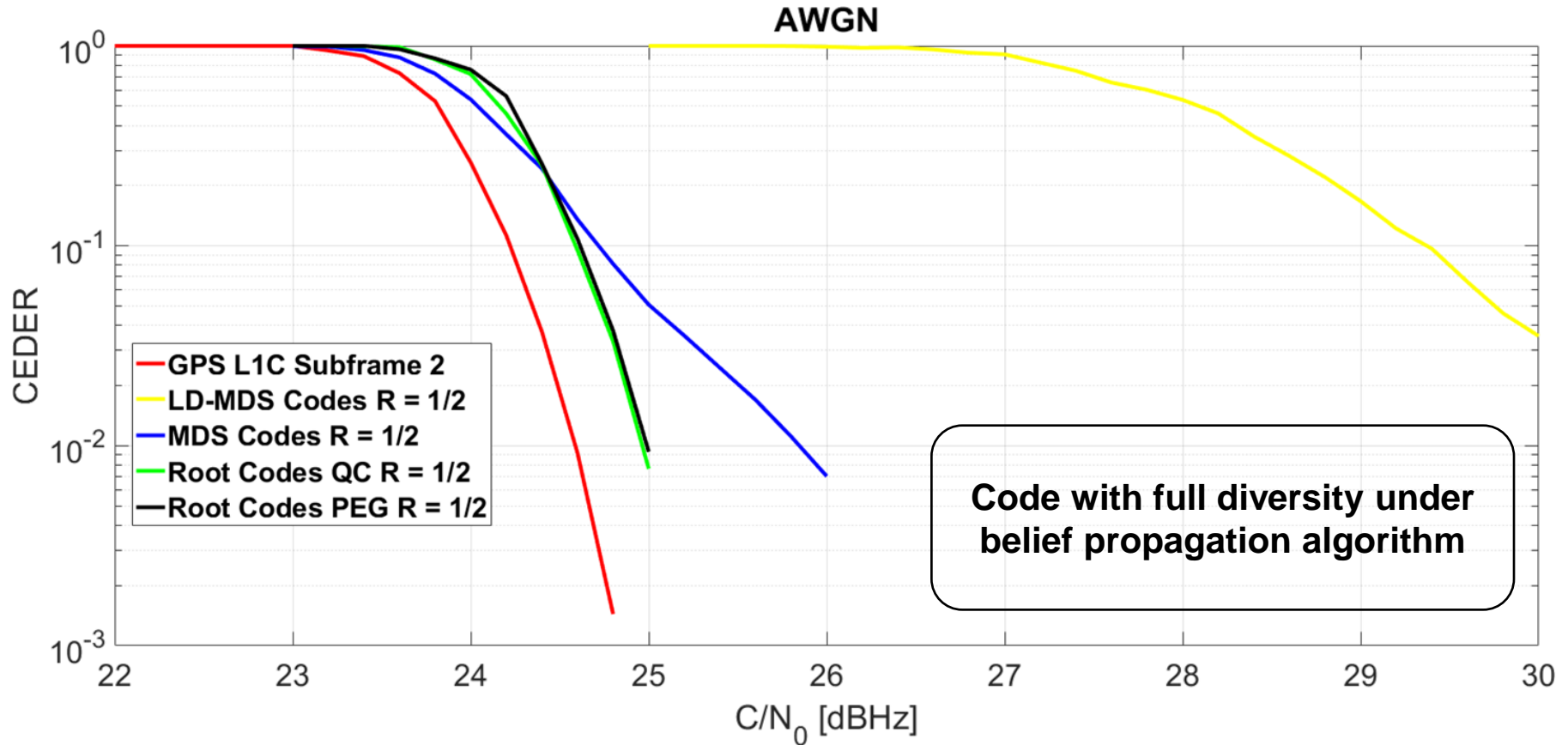
They have full diversity property under BP algorithm

Example:

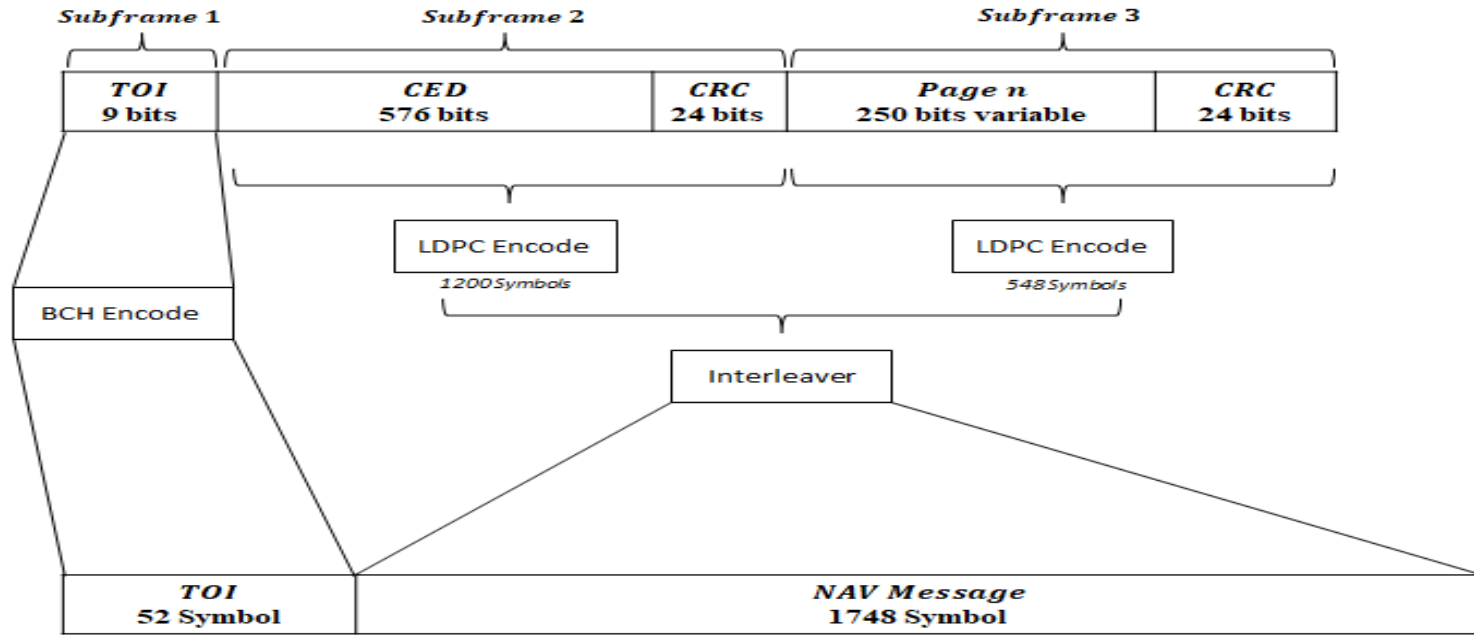


We don't need erasure algorithm → Running BP algorithm, we retrieve the information

Regular-Root codes

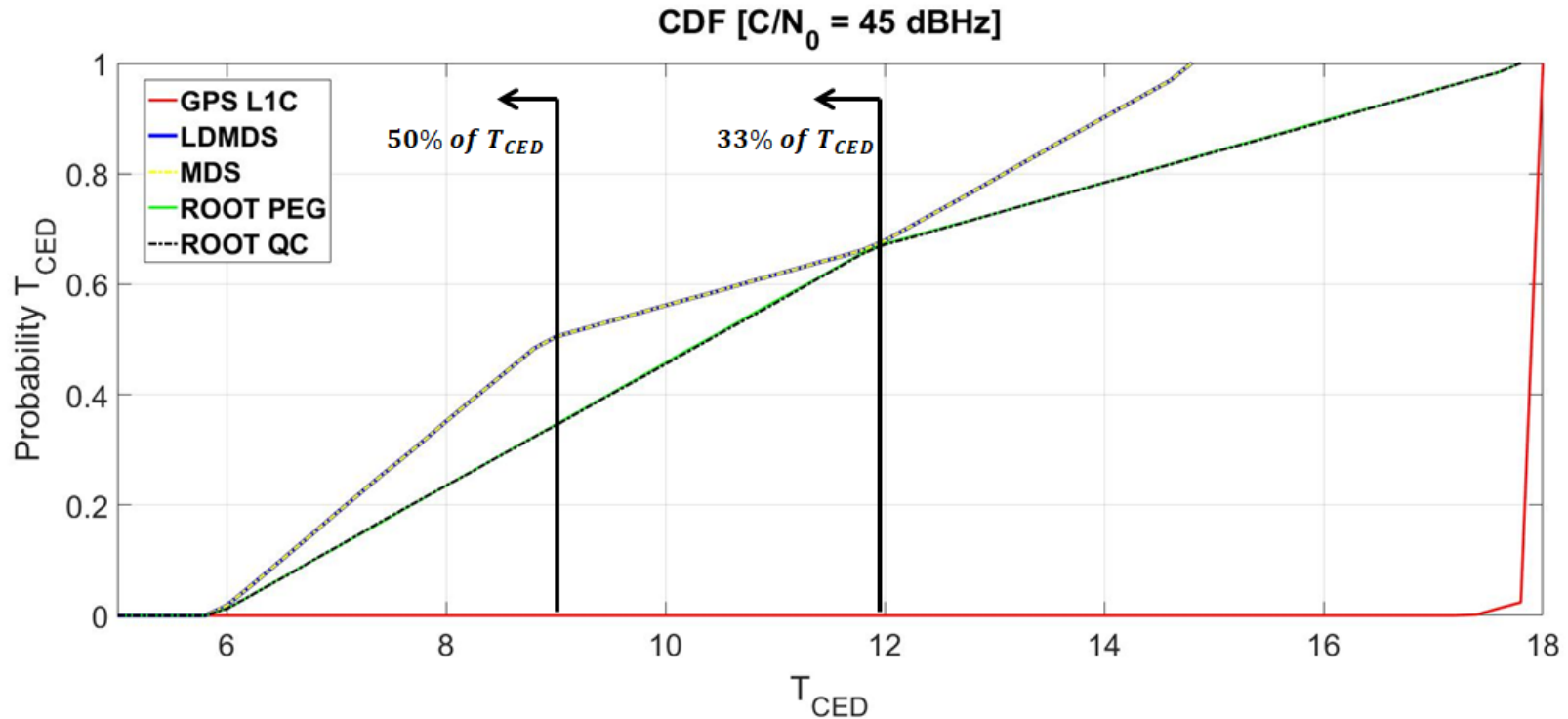


Cumulative Distribution Function (CDF)



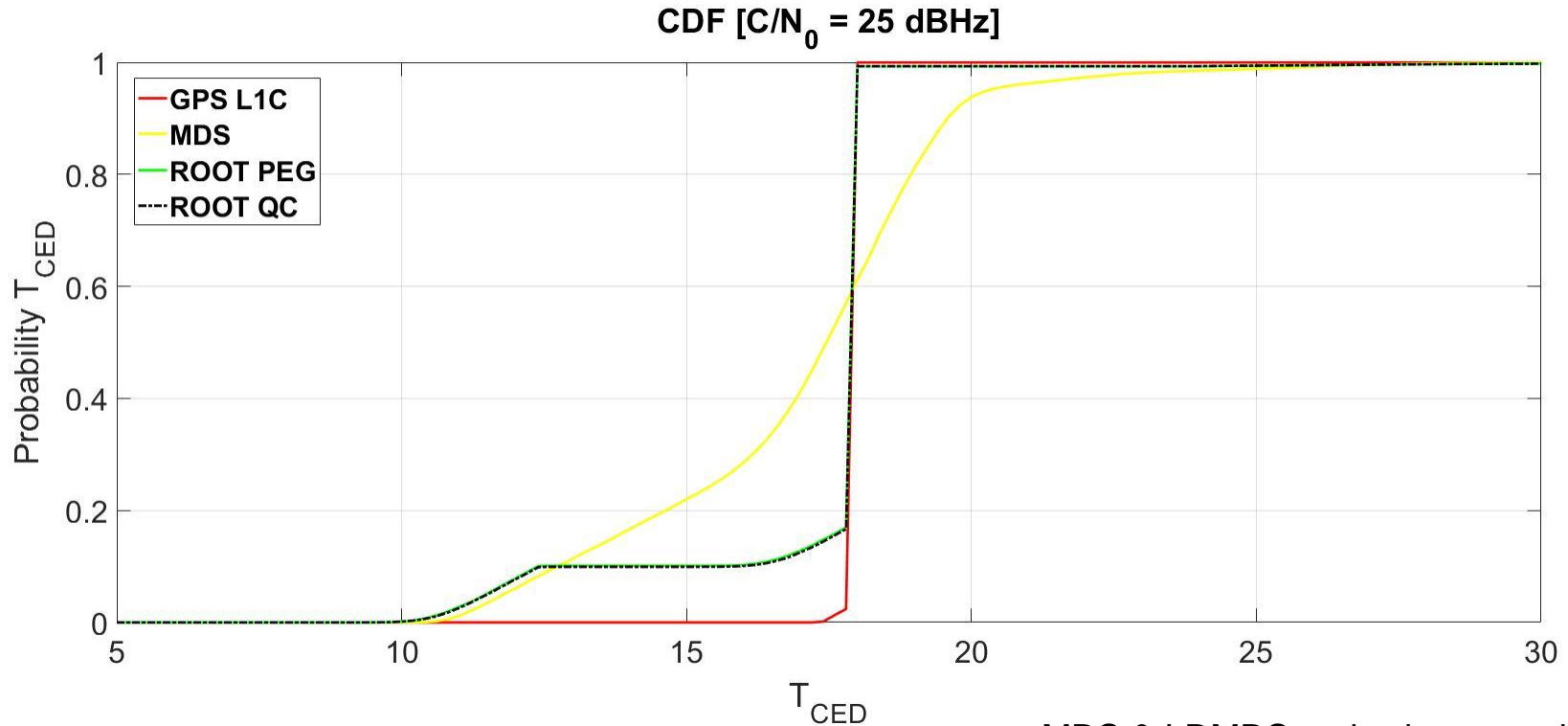
17,48 S

Cumulative Distribution Function (CDF)



Under good channel conditions, we reduce the T_{CED}

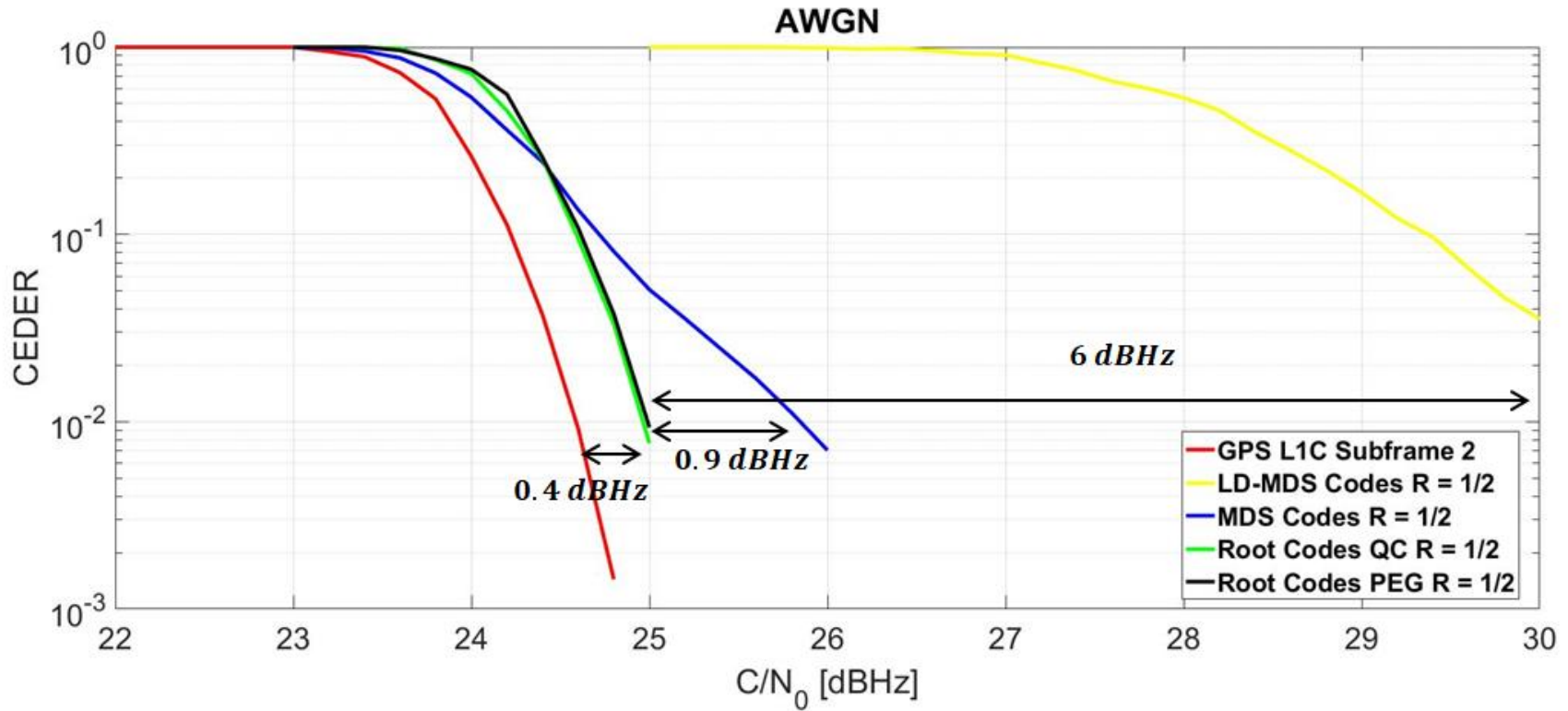
Cumulative Distribution Function (CDF)



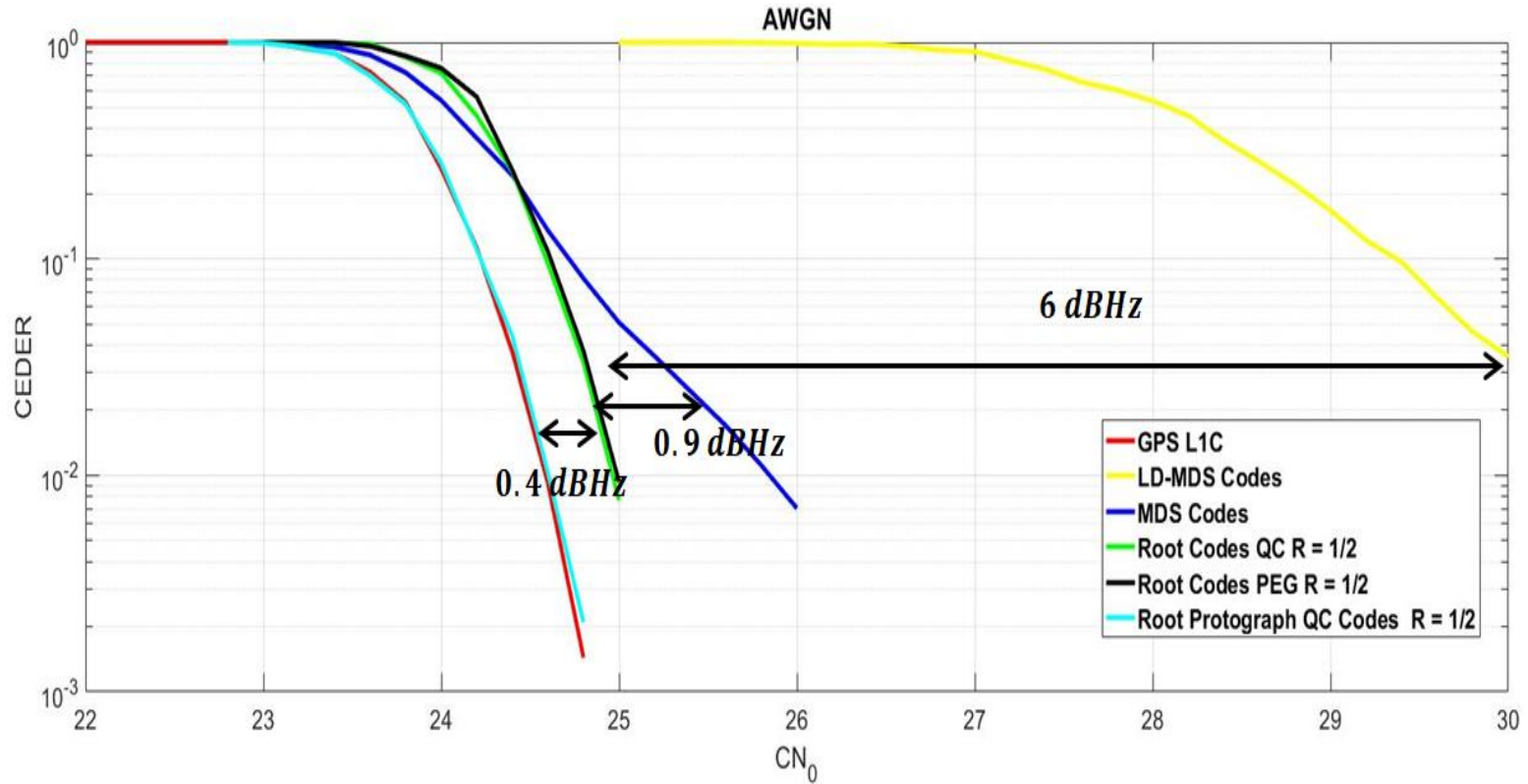
Under harsh channel conditions:

MDS & LDMS codes increase the T_{CED}

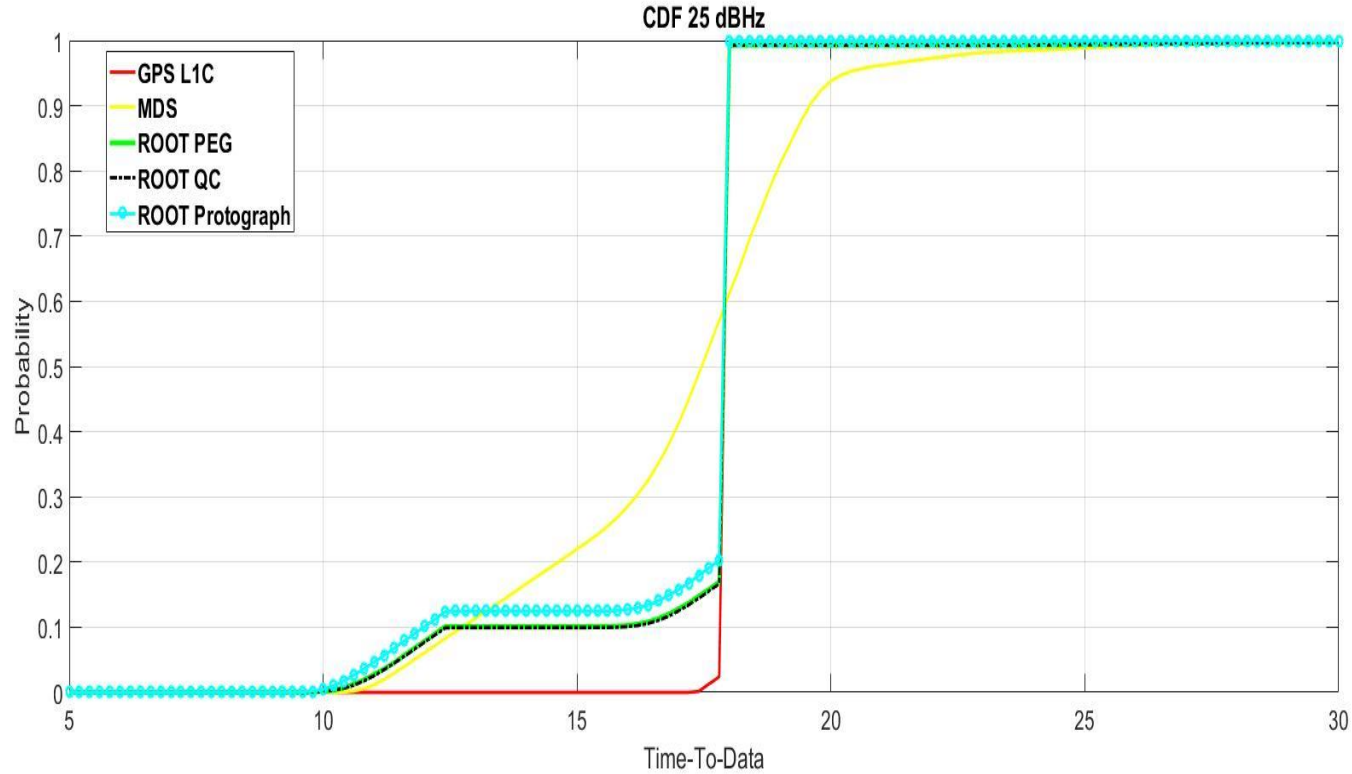
Root codes reduce the T_{CED}



Protograph-Root codes



Protograph-Root codes



- Introduction & background
- Design a new modulation for fast acquisition:
 - BCS
- Design new PRN codes for fast acquisition:
 - Random codes
- Co-design of the message structure and channel coding :
 - Maximum distance separable codes(MDS)
 - Full diversity Codes
- **Conclusion**
- Future Lines

- Objective : Design a new signal to improve the acquisition phase
 - To improve the receiver sensitivity and to reduce the TTFF*

- Results:

- BCS[-1,-1,-1,1,-1](1)

→ Improve of the receiver sensitivity

- Random Sequences PRN codes

→ Reduction of the TTFF and easing the acquisition phase vs GPS

- Regular root-codes:

- MDS property under BP algorithm

- Full diversity

→ High Reduction of the TTFF with good data demodulation vs GPS

- Introduction & background
- Design a new modulation for fast acquisition:
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 - Full diversity Codes
- Conclusion
- **Future Lines**

- Next step:
 - Use of protograph code to improve the channel coding
 - Rate compatible property
 - Multiplexing the new signal
 - How to compute the LLR in real scenarios
 - Work with M-ary modulation (CSK modulation)
 - Work with non-binary codes

thank you!



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